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# An Insect-Based Approach to the Dynamic Task Allocation Problem

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Anno Accademico 2003/2004

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# Abstract

La tesi si propone di sviluppare e implementare *Ant Task Allocation (ATA)*, un algoritmo basato sul modello di divisione del lavoro osservato in colonie di formiche per risolvere un problema di scheduling. Le prestazioni di *ATA* sono confrontate con quelle di altri algoritmi multi-agente presenti in letteratura.

La tesi sostiene che per diverse classi di istanze del problema e per una determinata funzione obiettivo, l'algoritmo sviluppato ottiene dei risultati migliori rispetto agli altri algoritmi considerati.

Il problema studiato è un problema di scheduling, non-deterministico, con macchine parallele e parte dell'informazione disponibile solo durante la risoluzione del problema stesso. Un ambiente industriale di verniciatura può essere portato come esempio di questo problema: dei camion escono da una linea di assemblaggio e devono essere assegnati a delle cabine di verniciatura. Le cabine possono avere le stesse caratteristiche oppure differire per la loro velocità di verniciatura. Un loro cambio di colore implica un ritardo temporale ed un costo. Il problema è complicato dal fatto che nessuna informazione sul colore dei camion da verniciare è conosciuta fino a quando questi non escono dalla linea di assemblaggio. L'obiettivo è quello di assegnare i camion alle cabine minimizzando il *makespan*, ovvero il tempo che intercorre dall'inizio della prima attività al completamento dell'ultima attività del sistema.

L'algoritmo proposto, che si basa sul lavoro di Cicirello *et al.* e sul modello a soglie presentato da Bonabeau *et al.* ispirato alla metodologia di suddivisione del lavoro osservata in colonie di insetti, definisce una serie di regole comportamentali delle cabine di verniciatura. Ogni cabina è considerata come un agente autonomo (formica) che richiede e vernicia dei camion (attività da svolgere). Il risultato è un sistema plastico ai cambiamenti dell'ambiente sperimentale dove gli agenti tendono a specializzarsi su un determinato tipo di lavoro in funzione delle loro caratteristiche e del loro stato.

Per sostenere la tesi, le prestazioni del sistema presentato sono state confrontate con quelle di altri algoritmi multi-agente presenti in letteratura tramite una analisi empirica su due classi di istanze del problema: una fabbrica di grosse dimensioni con cabine identiche ed una di medie dimensioni con cabine di differenti caratteristiche. La comparazione avviene tra *ATA*, la soluzione proposta da Cicirello *et al.*, un altro algoritmo insect-based di Campos *et al.*, un algoritmo market-based proposto da Morley ed un algoritmo non adattativo introdotto come punto di riferimento per il confronto delle prestazioni. Particolare attenzione è stata data alle condizioni sperimentali che hanno visto l'utilizzo di un generatore di istanze delle classi del problema, una ricerca dei parametri ottimali usando algoritmi genetici, e un'analisi statistica rigorosa.

Per completezza, l'analisi sperimentale mostra inoltre il contributo che ogni regola introdotta porta alla funzione obiettivo.



# Original contributions

I hereby declare that this thesis has not been submitted, either in the same or in different form to this or any other university for a degree. The described research work is based mostly on work carried out by myself in collaboration with Mauro Birattari and Shervin Nouyan. My research was carried out at the *Institut de Recherches Interdisciplinaires et de Développements en Intelligence Artificielle* at the *Université Libre de Bruxelles* under the supervision of Marco Dorigo. The results of all these studies has already been registered as technical report [14]. A part of this work is ready to be submitted to an international scientific journal.



# Acknowledgments

First of all, I would like to thank my supervisors Prof. N. Alberto Borghese and Prof. Marco Dorigo. I thank Prof. Borghese for enabling me to do my research thesis in Brussels and for his support from Italy. I thank Marco Dorigo for introducing me to the IRIDIA lab: it is a nice place with all I needed to develop this thesis.

A special thanks to Shervin Nouyan and Mauro Birattari, my research collaborators that helped me in this work. I thank Shervin, for introducing me to this interesting topic and for his permanent help. I thanks Mauro for his criticism, for the design of the experimental analysis and for his  $\LaTeX$  macros used to format this thesis.

I wish to thank all the friends with whom I have shared my time in Brussels. In particular I thank Elio, Max, Halva, Vito, Roderich, Tom, Christos, Fabiola, Michela, Stefano, Davide, Carlotta, Elisa and Roberta.

I want also to thanks Barbara, Monica, Matteo, Filippo, Brusa, Marta, Serena, Diego, Fra, Vitto and Gloria for encouraging me to do this important experience.

A very special thank goes to my family, Ernesto and Palmira, for their constant love and their care.

And finally a special thanks to Vera, for the love she gave me during this experience abroad.

Roberto Ghizzioli,  
October 2004





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# Chapter 1

## Introduction

The use of Multi-Agent Systems (MAS) is rapidly increasing in a variety of fields of computer science, engineering and artificial intelligence in the last years. A multi-agent system can be described as a loosely coupled network of agents interacting to collectively solve problems which are beyond the capabilities of each individual agent [12]. Agents are autonomous systems capable of adapting to changing environments and able to exhibit goal-directed behaviors [31].

Systems that reflect the previous definitions are for example insect colonies. Social insect colonies use intelligent and distributed methods to collectively solve complex problems. Cooperation among individual insects is largely self-organized and does not require any supervision. The collective behavior that emerges from a group of social insects is referred to as *swarm intelligence*. The research area that deals with applying swarm intelligence to various problems has come under increasing attention in the research community in the last years [10]. One of the early studies of swarm intelligence investigated the foraging behavior of ants. Ants lay trails of pheromone, a chemical substance that attracts other ants. Deneubourg *et al.* [9] showed that this process of laying a pheromone trail that others can follow, is a good strategy for finding the shortest path between a nest and a food source. In experiments with an Argentine ant species, Deneubourg *et al.* constructed a bridge with two branches, one twice as long as the other, separating the nest from a food source. Within few minutes the ants mostly selected the shorter branch. Based on the idea of pheromone laying and following, Dorigo *et al.* [11] developed a way to solve the well known and NP-hard<sup>1</sup> Traveling Salesman Problem (TSP). The TSP is the problem of finding the shortest route that goes through a given number of cities exactly once. The algorithm, implemented by Dorigo *et al.* has obtained near optimal solutions.

In this thesis our interest is in using multi-agent algorithms to solve the Dynamic Task Allocation (*DTA*) problem. The *DTA* problem is an online, non-deterministic scheduling problem, that is, a decision-making process for assigning

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<sup>1</sup>For a definition of the concept of NP-Hardness and NP-Completeness we refer the reader to [13].

tasks to agents working in parallel. Each task belongs to a particular type and if a working agent changes the type of task it performs, a setup is required and a given cost is incurred. In the *DTA* problem different agents can have different processing times for different task types. If this is the case, the *DTA* problem is said heterogeneous; otherwise, if all the agents are identical, the problem is said homogeneous (*DTA<sub>Hom</sub>*). The objective for this problem is to minimize the makespan, that is, the time until all tasks in the system have been processed.

Different work has been done using multi-agent algorithms on the homogeneous case of the problem. Most of the proposed algorithms use paradigms based on the *specialization* concept, where agents tend to specialize for one type of task, to avoid unnecessary reconfiguration and in this way increase the efficiency of the system. Morley [18] is the first one that solved a painting problem similar to the homogeneous case of the *DTA* problem. His algorithm was adopted in the GM facility and was found that his system performs 10% better than the previously used centralized scheduler. Later, Campos *et al.* [6] proposed to solve the same problem with an insect-based approach. Subsequently, Cicirello *et al.* [7] proposed another insect-based algorithm introducing concepts not considered by Campos *et al.*

In this thesis, we present *Ant Task Allocation (ATA)*, an algorithm for the homogeneous case of the problem based on the work of Cicirello *et al.* The algorithm of Cicirello *et al.*, especially for problems in which demands change dynamically, often takes much time to re-adapt or does not succeed to re-adapt at all. In order to overcome this problem we propose some modifications and additional rules to speed up the adaptation process.

Applying these algorithms to the heterogeneous case of the *DTA* problem, we found that they perform poorly because the agents do not consider their process speed to perform a task. Therefore, we propose a *Different Process Speed (DPS)* rule applicable to all the considered insect-based algorithms. This rule is inspired by division of labor as observed in different castes of *Pheidole* ants.

We compare all presented algorithms on the *DTA* problem. Additionally, we introduce a non-adaptive algorithm in the experimental analysis in order to have a performance reference. The comparison considers two possible real-world situations: a big painting factory with identical agents and a medium dimension factory with two heterogeneous subsets of agents. Particular attention has been paid to the experimental conditions; in fact, we have used two instance generators in order to obtain the two classes of instances of the problem and we have done a rigorous parameters tuning for each used algorithm. Furthermore, a statistical analysis has been done to study the data obtained. We will show that our algorithm achieves the best results for both the considered class of homogeneous and heterogeneous problems. Moreover, we will show that all adaptive algorithms in all situations achieve better results than the non-adaptive algorithm. Again, Campos' *et al.* algorithm does not obtain good results in both the experiments

but we are grateful to him because his work has the merit of having introduced the insect-based approach to solve this problem. Moreover, the performance of the insect-based algorithms are ranked according to the time they was made. In fact the algorithm of Campos' *et al.* does not obtains good results, the algorithm of Cicirello *et al.* gives a significant improvement to the performance obtained by Campos' *et al.* as they show in paper [7] and our algorithm improves again the results of the solution of Cicirello *et al.*

Another set of experiments deals with the analysis of the proposed rules. First of all we show that *ATA* with all the introduced rules performs better than the original algorithm of Cicirello *et al.* Moreover, we observe that one of the proposed rules gives a large contribution to reduction in the makespan, two others a significant contribution to it and the last one does not give any apparent contribution to the results. Finally, we show that the *DPS* rule improves the performances of all the insect-based algorithms on the heterogeneous case of the *DTA* problem.

In Chapter 2 we give a formal description of the *DTA* problem and use the metaphor of a painting facility to describe it in a simple way. Chapter 3 presents the related work for the homogeneous case of the *DTA* problem. We present two approaches: the market-based approach with the algorithm of Morley and the insect-based approach with the algorithms of Campos *et al.* and Cicirello *et al.*. Afterwards, Chapter 4 introduces *ATA*, our algorithm for the *DTA<sub>Hom</sub>* problem. In Chapter 5 we describe the *DPS* rule which is applicable to the insect-based algorithms in the heterogeneous case of the problem. Chapter 6 details the experimental setup and the instance generators. Furthermore, a summary of the algorithms and of the parameter is given. In the second part of this chapter, we analyze the obtained results. Finally, we conclude in Chapter 7.



# Chapter 2

## Problem definition

The problem considered here is a particular non-deterministic scheduling problem that we refer to as the Dynamic Task Allocation (*DTA*) problem. This problem is a decision-making process for assigning tasks to parallel working machines. In the *DTA* the machines differ in their process speed. Moreover, tasks information is only known at execution time. A very similar problem, with identical machines, was presented and solved by Morley [18] for painting trucks at General Motors.

The *DTA* problem can be described by considering a painting factory environment.

**Painting facility.** Trucks roll off an assembly line at the end of which there is a storage where each truck waits to be assigned to a painting booth. The number of available colors is fixed and a truck's color is predetermined by a customer order. The distribution of colors of trucks and the truck release dates are not specified.

A painting booth is an agent able to paint with all the available colors. Booths may be identical or may have different process times for the same type of tasks. This situation may happen for example in a factory with old and new machines, where the new ones require less time to accomplish a same task. Another possibility is that a set of agents do some work faster than another and vice versa. Moreover, each booth has a fixed queue length which can be filled by trucks. If the color of a painting booth must be changed, a setup time is necessary. For example, if a booth is applying red and the next truck to be processed by that painting booth requires white, a fixed flush time is taken. If no setup is necessary, the booth starts immediately to paint the next truck in its queue. A setup may also be related to a monetary cost that for example is the amount of paint lost during a swap.

The objective of this problem is to assign trucks to painting booths minimizing the makespan, that is, the completion time of the last truck in the system. We also analyze the number of setups and the storage dimension that should be kept as low as possible.

## 2.1 Dynamic task allocation (*DTA*) problem

According to Pinedo [20] we formalize the scheduling problem introduced by the following notation

$$\langle Qm|r_j, s_{j,h}|C_{MAX} \rangle, \quad (2.1)$$

where each variable has the following meaning:

- **Machines in parallel**  $Qm$ : in the system there are  $m$  machines in parallel that are in charge of  $m$  booths in the paint facility. Machines may have different process times for different types of tasks. Groups of machines can be grouped in different subsets  $S_i$ . The process times of a subset  $S_i$  for the types of tasks  $c_j$  is given by  $t_{proc}(S_i, c_j)$ . The setup time  $t_{setup}$  is identical for all the working machines. Furthermore, each machine  $k$  has a queue that can be filled with up to  $q_k$  tasks. If all machines have the same processing time  $t_{proc}$  for all types of tasks, we refer to the homogeneous case of the problem ( $DTA_{Hom}$ ).
- **Release date**  $r_j$ : this is the time at which a task  $j$  is released to the painting facility. The value of  $r_j$  is not available at the beginning of the experiment. It is the earliest time at which the task  $j$  can start being processed. Each task  $j$  requires a single operation and may be processed on any one of the  $m$  machines. Furthermore, each task  $j$  belongs to a particular type  $c_j$  which is the color to be painted and also this information is not available at the beginning of the experiment.
- **Sequence dependent setup times**  $s_{j,h}$ : represents the sequence dependent setup time between two tasks  $j$  and  $h$ . If  $c_j = c_h$ , no setup is required and  $s_{j,h} = 0$ . This means that the respective machine can immediately start processing task  $h$  after having finished to process task  $j$ . If  $c_j \neq c_h$ , a configuration time  $t_{setup}$  is needed. The setup time between task  $j$  and task  $h$  is independent of the machine.
- **Makespan**  $C_{MAX}$ : the objective of the *DTA* problem is to minimize the makespan that is the time until all tasks in the system have been processed.

In the *DTA* problem, the task generation process is not specified. For instance, the release dates and the types of the tasks may be distributed exponentially or normally. This distributions may vary dynamically so that at a random time the probability mix changes and the machines need to adapt to the new environment. It also may happen the extreme case of all tasks being create before the scheduling process start. This last example would make the *DTA* instance a very simple scheduling problem requiring only a simple algorithm to optimize a schedule because everything is known a priori.



# Chapter 3

## Related work

In the previous chapter we used a painting facility as a real world example of the  $DTA_{Hom}$  problem. This example originates from Morley [18], who was given the task of optimizing a scheduler for a General Motors truck painting facility. Morley used a decentralized market-based approach that, compared to the previously used centralized scheduler, improved the performance in terms of decreasing the amount of paint lost. In the following section we give a short overview of market-based algorithms for problems that are related to the  $DTA_{Hom}$  problem. In particular, we detail Morley's approach.

Independently of each other, Campos *et al.* [6] and Cicirello *et al.* [7] used similar insect-based approaches to solve the same problem. They were inspired by a threshold model proposed by Bonabeau *et al.* [2, 3] and Theraulaz *et al.* [27]. In Section 3.2 we first introduce the threshold model and then explain the two approaches.

### 3.1 Market-based approach

Market-based approaches are often used for coordinating asynchronous scheduling operations in the face of imperfect knowledge [8, 17, 16]. The decision process is based on a decentralized bidding mechanism where autonomous agents bid for a task or a resource, which is then assigned to the agent with the highest bid. The agents dynamically adjust their bids according to their capability to solve a task or according to the availability of a resource.

For example, Waldspurger *et al.* [29] presented a computational system called *Spawn*, in which each task bids for the use of machines on a network. According to its priority, each task is given a certain budget, which it has to use such that it will be assigned to the resources it requires. Prices are adjusted dynamically and are based on the demands of other tasks.

Another example is given by Schwartz *et al.* [25] that use the bidding mechanism for data allocation of self-motivated data servers with no common pref-

erences and no central controller. The location of each data unit is determined using a bidding mechanism where the server bidding the highest price for obtaining the data will actually obtain it. This market-based approach yields an efficient and fair solution, a simple implementation and the bidders are motivated to offer efficient prices.

Clearwater *et al.* [15] also use a market-based approach for a thermal resource distribution problem: computational agents that represent individual temperature controllers bid to buy or sell cool or warm water air.

All these examples show that market mechanisms provide methods to deal with coordinating asynchronous operations in the face of imperfect knowledge. A computational system set up along market rules can allow the system as a whole to adapt to changes in the environment or disturbances to individual members. Additionally, the price mechanism behind this approach simplifies the design of adaptive algorithms.

### 3.1.1 Morley's algorithm

The following algorithm definition originates from the paper of Campos *et al.* [6]. In fact, the algorithm developed by Morley is a manufacturing application and many details are protected.

Morley [18] proposed a market-based algorithm to solve an example of the homogeneous case of the *DTA* problem which was applied to a General Motors factory. We refer to his algorithm as *Market-Based Approach (MBA)*. In his market-based approach booths bid for trucks to paint them. For each booth the intensity of the bid for a particular truck is based on the amount of time and the additional costs that would be related to an assignment. If the queue of a booth is full, it does not participate to the bidding process. Morley proposed a bid function applied to each booth that considers the importance of the tasks, the color of the presented task, and the state of the booth. More precisely, if we consider a task  $j$  of color  $c_j$  that is in the storage, a booth  $k$  that does not have a full queue participates in the bidding process with a range of values given by:

$$B_k(j) = \frac{P * w_j * (1 + C * e(k, j))}{\Delta T_k(j)^L}, \quad (3.1)$$

where  $w_j$  gives the importance of the task,  $e(k, j)$  is a function that is 1 if the color of the last truck in the queue is equal to  $c_j$ , and 0 otherwise.  $P$ ,  $C$ , and  $L$  are parameters that weight each component.  $\Delta T_k(j)$  is the time until task  $j$  starts to be painted, and is determined by the following equation

$$\Delta T_k(j) = q * t_{proc} + n * t_{setup} + t_{working}, \quad (3.2)$$

where  $q$  is the number of trucks in the queue of booth  $k$ ,  $t_{proc}$  is the time required to paint one truck,  $n$  is the number of setups between trucks in the booth's queue,

$t_{setup}$  is the time required for a setup, and  $t_{working}$  is the time necessary to finish the truck currently being painted.

The assignment process is very simple. For all trucks each booth with space in its queue bids for them according to Equation 3.1 and the respective truck is assigned to the end of the queue of the highest bidder. If all the queues are full no booth can bid and the truck stays in the storage. If more than one booth submits the same highest bid, the respective truck is assigned to the booth that requires no setup to paint it. In the case that all competing booths require a setup, the winner is chosen randomly. If none of the booths requires a setup, the truck is assigned to the booth with the shortest queue size or, in case all the booths have the same queue length, it is assigned randomly.

## 3.2 Insect-Based approach

Campos *et al.* [6] and Cicirello *et al.* [7] used an insect-based approaches to solve the  $DTA_{Hom}$  problem which are inspired by the methodology of division of labor in social insect. Insect societies perform different activities simultaneously exploiting specialized individuals. This *parallelism* is undoubtedly more efficient than sequential task performance by unspecialized workers because *individual specialization* leads to a higher grade of colony efficiency as specialized individuals don't switch between one type of task and another, a process that often requires time. Moreover, a specialized individual can perform a type of tasks more efficiently.

A key feature of division of labor is *plasticity*. The ratios of workers performing the different tasks can vary in response to internal and external challenges. Factors such as food availability, climatic conditions or phase of colony development influence the specialization of the colony's workers. In the *Pheidole* ant species, for example, there are minor workers that are smaller and morphologically distinct from major workers. Minor and major workers tend to perform different tasks: while majors cut large preys and defend the nest, minors feed the brood or clean the nest. Wilson [30] showed experimentally that when removing minors, majors get engaged in the tasks usually performed by minors to replace them.

**The fixed threshold model** In order to explain Wilson's [30] observations, Bonabeau *et al.* [4] have developed a simple model that relies on response threshold [22, 21]. The idea behind the fixed threshold model is that each individual has a *threshold* value for every kind of *task* available in an environment. A threshold represents the level of specialization of an agent for a particular task. A task emits a *stimulus* to attract the individuals' attention. Based on the stimulus, an individual will or will not accept to start performing the respective task. The higher the intensity of a stimulus the higher the attraction toward workers to

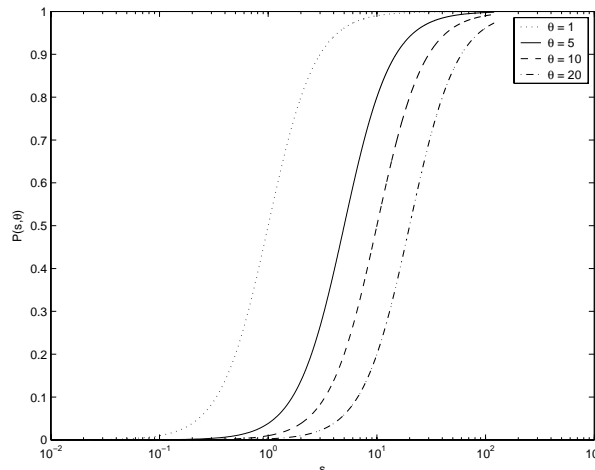


Figure 3.1: Response curve  $P(s, \theta)$  with different thresholds.

accept that task. This model is said to be with *fixed* thresholds because these thresholds do not change over time.

The first question that we have to answer is: how do we formally define a response threshold? Assume that  $m$  tasks need to be performed. Each task  $j$  is associated with a stimulus  $s_j$ , the level of which increases if it is not satisfied. Let us assume that there are  $N$  agents, denoted by  $i$ , with *response threshold*  $\theta_{i,j}$  ( $i = 1, \dots, N$ ) for each task  $j$ . In the threshold model, individual  $i$  engages in task  $j$  with probability

$$P(s_j, \theta_{i,j}) = \frac{s_j^2}{s_j^2 + \theta_{i,j}^2}. \quad (3.3)$$

This equation shows that for  $s_j \ll \theta_{i,j}$  the probability of an individual  $i$  to be engaged in task  $j$  is close to 0 and for  $s_j \gg \theta_{i,j}$  the probability is close to 1. Therefore, agents  $i$  with a lower threshold  $\theta_{i,j}$  are more likely to respond at a lower level of stimulus  $s_j$ .

The fixed threshold model assumes that agent's thresholds are fixed over time and so their level of specialization for a given task does not change in time. As a consequence, this model does not take into account the plasticity characteristic of the colony because it assumes that individuals are differentiated by their preassigned threshold values. Therefore, it is valid only over sufficiently short time scales, where thresholds can be considered constant. Finally, the model is not consistent with experiments with honey bees [23, 5], showing that aging and/or learning play a role in task allocation.

**The dynamic threshold model** In order to take these limitations into account, Theraulaz *et al.* [27] extended the threshold model by allowing thresholds

to *vary in time* following a simple *reinforcement* process: the threshold associated to a task decreases when the corresponding task is performed, and increases otherwise.

Let  $\xi$  be the coefficient that describes *learning* (specialization) and  $\varphi$  be the coefficient that describes *forgetting* characteristics of an insect colony. If we consider a time-incremental model, individual  $i$  specializes when performing task  $j$  during a time period of duration  $\Delta t$  by changing its threshold as follows:

$$\theta_{i,j} \rightarrow \theta_{i,j} - \xi \Delta t, \quad (3.4)$$

and it forgets if it does not perform task  $j$  during a time period of duration  $\Delta t$  by changing its threshold as follows:

$$\theta_{i,j} \rightarrow \theta_{i,j} + \varphi \Delta t. \quad (3.5)$$

Now, let  $x_{i,j}$  be the fraction of time spent by individual  $i$  in task  $j$ : within  $\Delta t$ , individual  $i$  performs task  $j$  during time  $x_{i,j} \Delta t$ , and other tasks during  $(1 - x_{i,j}) \Delta t$ . Let  $\xi$  and  $\varphi$  be identical for all tasks, and the dynamics of  $\theta_{i,j}$  be restricted to an interval  $[\theta_{min}, \theta_{max}]$ . Therefore, threshold values vary continuously in time according to:

$$\frac{\partial \theta_{i,j}}{\partial t} = [(1 - x_{i,j})\varphi - x_{i,j}\xi] \Theta(\theta_{i,j} - \theta_{min}) \Theta(\theta_{max} - \theta_{i,j}), \quad (3.6)$$

where  $\Theta(\cdot)$  is the Heaviside function with  $\Theta(y) = 0$  if  $y < 0$ ,  $\Theta(y) = 1$  if  $y \geq 0$ .

The probability of an individual  $i$  to be engaged in task  $j$  is still described by equation 3.3, but now  $\theta_{i,j}$  is dynamic in time and therefore:

$$P(s_j(t), \theta_{i,j}(t)) = \frac{s_j^2(t)}{s_j^2(t) + \theta_{i,j}^2(t)}. \quad (3.7)$$

As explained above,  $x_{i,j}$  is the fraction of time spent by individual  $i$  in performing task  $j$ . Its value increases according to the threshold  $\theta_{i,j}$  of agent  $i$  for task  $j$ .  $x_{i,j}$  varies in time according to:

$$\frac{\partial x_{i,j}}{\partial t} = P(s_j, \theta_{i,j}) \left(1 - \sum_{k=1}^m x_{i,k}\right) - p x_{i,j} + \Psi(i, j, t), \quad \forall k \neq j, \quad (3.8)$$

where  $1 - \sum_{k=1}^m x_{i,k}$  is the fraction of time potentially available for performing tasks. The term  $p x_{i,j}$  expresses that an active individual gives up task performance and becomes inactive with probability  $p$  per unit time (identical for all workers and all tasks). The average time spent by an individual in task  $j$  performance before giving up this task is  $1/p$ .  $\Psi(i, j, t)$  is a centered Gaussian stochastic process with variance  $\sigma^2$ , which is uncorrelated in time, among individuals and among tasks.

For simplicity, the stimulus dynamics for a task  $j$  increases at a fixed rate per unit time if no agent bids for it. The differential equation that describes the variation of  $s_j$  in time is

$$\frac{\partial s_j}{\partial t} = \delta - \frac{\alpha}{N} \left( \sum_{i=1}^N x_{i,j} \right), \quad (3.9)$$

where  $\delta$  is the increase in stimulus intensity per unit time, and  $\alpha$  is a scale factor measuring the efficiency of task performance. It is assumed that both factors are identical for all tasks, and that  $\alpha$  is fixed and identical for all individuals.

In reality, however,  $\alpha$  could vary as a result of specialization. The amount of work performed by active individuals is again scaled by the number of individuals  $N$ .

### 3.2.1 Campos' algorithm

Campos' *et al.* [6] solved the  $DTA_{Hom}$  problem with an algorithm based on the dynamic threshold model as shown in the previous chapter. They developed this algorithm to show similarities between the *insect-based* approach and the *market-based* approach. We call their algorithm *Ant-Based Approach (ABA)*. In this approach agents are in charge of booths and autonomously bid to paint trucks. In Campos' model, a stimulus  $s_{c_j}$  is associated to the color  $c_j$  of a truck  $j$ . Each agent  $k$  has a threshold value  $\theta_{k,c_j}$  for each available color. The stimulus  $s_{c_j}$  for each color is given by the sum of the stimuli of the unassigned tasks for each particular color. The equation that describes the stimulus demand is:

$$s_{c_j} = \sum_i s_i \delta(c_i - c_j), \quad (3.10)$$

where  $c_i$  is the color of truck  $i$  waiting in the storage and  $c_j$  is the color of the considered truck  $j$ .  $\delta(\cdot)$  is the Dirac function and the sum is taken over all trucks.

The probability of the booth  $k$  to get engaged in task  $j$  is given by:

$$P(s_{c_j}, \theta_{k,c_j}) = \frac{s_{c_j}^2}{s_{c_j}^2 + \alpha \theta_{k,c_j}^2 + \Delta T^{2\beta}}, \quad (3.11)$$

where  $c_j$  is the color of truck  $j$  and  $\theta_{k,c_j}$  is the threshold of agent (booth)  $k$  for color  $c_j$ .  $\alpha$  and  $\beta$  are parameters and  $\Delta T$  is the waiting time necessary before the truck starts to be painted by that booth.  $\Delta T$  is computed like in equation 3.2. If there are no bidders because all the queues are full the truck stays in the storage. For this algorithm, values of  $P(s_{c_j}, \theta_{k,c_j})$  for different agents are compared and the task is assigned to the booth with the highest value.

Only when a truck  $j$  is assigned to booth  $k$ , the threshold values are updated for all booths.  $\theta_{k,c_j}$  decreases by an amount  $\xi$ :

$$\theta_{k,c_j} \rightarrow \theta_{k,c_j} - \xi, \quad (3.12)$$

and the thresholds  $\theta_{m,c_j}$  of all other paint booths for color  $c_j$  increase by an amount  $\varphi$

$$\theta_{m,c_j} \rightarrow \theta_{m,c_j} + \varphi, \forall m \neq k. \quad (3.13)$$

Variations of  $\theta_{*,c_j}$  take place within the bounds  $\theta_{min}$  and  $\theta_{max}$ . Equation 3.12 expresses the fact that booth  $k$  tends to specialize on color  $c_j$  because it increases its probability of responding to a truck with color  $c_j$  by decreasing its response threshold  $\theta_{k,c_j}$ .

### 3.2.2 Cicirello's algorithm

Cicirello *et al.* [7] proposed a similar algorithm to solve the  $DTA_{Hom}$  problem called *R-WASP* that is also inspired by the dynamic threshold model.

The algorithm incorporates aspects which have been ignored by Campos. In particular, in Cicirello *et al.*'s algorithm, each task  $j$  in the system sends to all agents a stimulus  $s_j$  that is equal to the length of time the task is already waiting to be assigned to an agent and does not depend on its color.

Campos' algorithm uses the probability function to determine the booth to assign the truck. Cicirello *et al.*'s model instead uses  $P(s_j, \theta_{k,c_j})$  as a *pre-disposition* to respond to a stimulus. Therefore,  $P(s_j, \theta_{k,c_j})$  represents the probability for a booth to bid for a task. In the algorithm of Cicirello *et al.*, the pre-disposition to respond to a stimulus is given by:

$$P(s_j, \theta_{k,c_j}) = \frac{s_j^2}{s_j^2 + \theta_{k,c_j}^2}, \quad (3.14)$$

where  $c_j$  represents the color or the type of task  $j$ .

Furthermore, in Campos' approach, *thresholds* are updated only when a truck is assigned to a paint booth and that rule involves only thresholds of the respective color. In Cicirello *et al.*'s approach, each agent  $k$ , at each time step, updates its own thresholds  $\theta_{k,*}$  according to the following rules. At each time step, if the agent  $k$  is processing or setting up for a task  $j$  of color  $c_j$  the agents' thresholds are updated according to:

$$\theta_{k,c_j} \rightarrow \theta_{k,c_j} - \xi, \quad (3.15)$$

$$\theta_{k,c_i} \rightarrow \theta_{k,c_i} + \varphi, \forall i \neq j. \quad (3.16)$$

Otherwise, if the agent  $k$  is currently not processing any task, a third update rule is used for each threshold:

$$\theta_{k,c_i} \rightarrow \theta_{k,c_i} - \delta^t, \forall i, \quad (3.17)$$

where  $t$  represents the number of time steps in which the agent is already idle. The rule given in Equation 3.17 increases the value of  $P(\theta_{k,c_j}, s_j)$  to encourage an idle agent  $k$  to take whatever tasks it can get rather than remaining idle.

When two or more agents of the colony want the same task, they interact with each other in a *dominance contest*. If this interaction takes place, the agent with the higher social rank has a higher probability of dominating in the challenge. Through such interactions, insects within the colony self-organize into a *dominance hierarchy*. The dominance contest rules are applied if two or more agents respond positively to the same stimulus. In this case there is a kind of challenge between bidders and the winner is assigned the task. The idea is that each participant  $k$  has a force value  $F_k$ :

$$F_k = 1 + T_{proc} + T_{setup}, \quad (3.18)$$

where  $T_{proc}$  is the sum of the processing times  $t_{proc}$  for all the tasks in the queue of booth  $k$  and  $T_{setup}$  is the sum of their setup times  $t_{setup}$ . For a booth  $k$ , a lower force value  $F_k$  corresponds to a shorter queue and leads to a higher probability to win in a dominance contest. The rule to determine the probability for agent  $k$  to win against all the others competitors, is:

$$P(F_1, \dots, F_n) = \frac{\sum_{i \neq k}^n F_i^2}{(n-1) \sum_{i=1}^n F_i^2}. \quad (3.19)$$

If more than one agent competes for a given task, a single dominance contest is used to determine the winner.



# Chapter 4

## *ATA*: An improved algorithm for the homogeneous case

The agent-based algorithm proposed by Cicirello *et al.* shows a good level of specialization of the paint booths. This characteristic is desirable because it avoids unnecessary reconfigurations. The way the solution is achieved is completely distributed and no global information is required. We used the algorithm of Cicirello *et al.* initializing all working agents with the same threshold for all types of tasks.

In general, we observed that during the experiment the agents become specialized in one type of task and the performances of this algorithm are better than these obtained by one of the non-adaptive algorithms. However, we have observed that *R-WASP* requires some amount of time to initially adapt to the product mix as well as to dynamically re-adapt to a changing product demand. For example, Cicirello *et al.* consider in their experiments a case with two types of task, an asymmetric probability distribution and a product mix that changes at the half of the simulation. They show that the adaptation process to the new probability mix takes more than one third of the experimental time.

In order to overcome this problem we propose three modifications on the original algorithm and one additional rule to speed up the adaptation process. We call this improved algorithm *Ant Task Allocation (ATA)* and specify it in the following two sections. Afterwards, in Section 4.3 we show the plasticity of *ATA* in a particularly dynamic environment by discussing an example.

### 4.1 Modifications of existing rules

*Threshold Update Rules (TUR)*: The update rules proposed by Cicirello *et al.* depend on the type of the task (the color  $c_j$ ) which is currently used by a booth. We remark that an agent may have a queue of several tasks behind itself. These tasks in the queue are not necessarily of a same type. For example, an agent might be processing a task of type 1 and have only one task in its queue that is

of type 2 like in Figure 4.1. This means that, as long as the task of type 1 is not finished, the corresponding threshold for 1 is decreased and the threshold value for 2 is increased. If the agent is offered two tasks, one of type 1 and one of type 2, the probability to take the task of type 1 is higher than the probability to pick task 2. This is not desirable because it can cause additional setups. We have chosen to modify the update rules by letting the last task in an agent's queue determine which threshold values are updated in order to reduce the number of necessary setup and consequently, the makespan.

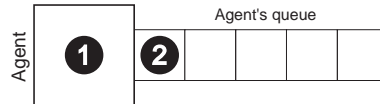


Figure 4.1: This agent is currently processing a task of type 1 and in its queue there is a waiting task of type 2.

*Calculation of the Force Variable (CFV):* The dominance contest introduced by Cicirello *et al.* tries to find a good solution to choose among several booths competing for a same task. The force value is defined as the sum of the process times and setup times of the tasks waiting in the queue of a booth. Figure 4.2 shows a situation where two agents with the same queue length bid for the same task. In the algorithm of Cicirello *et al* the probability to win in the dominance contest is the same. This does not take into account a possibly required setup for the task they are bidding for. We modify the force value according

$$F_k(j) = 1 + T_{proc} + T_{setup} + t_{setup,j}, \quad (4.1)$$

where  $t_{setup,j}$  represents the setup time between the last task in the booth's queue and the current truck  $j$ .

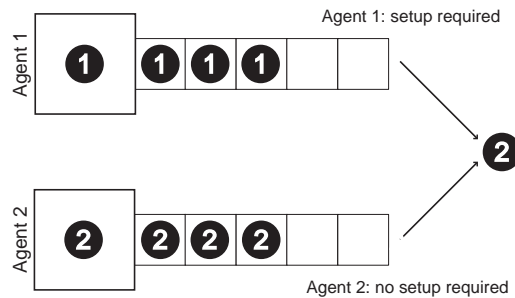


Figure 4.2: Two agents with the same queue length that bid for the same task.

*Dominance Contest (DOC):* Using the dominance contest rule as specified in Equation 3.19, the more machines compete with each other in a dominance

contest, the smaller are the differences between the probabilities to win. In general the probability for one competitor to win a dominance contest with  $n$  competitors is never higher than  $\frac{1}{n-1}$ . In order to avoid this, we introduce this new rule:

$$P_k(F_1, \dots, F_n) = \frac{\frac{1}{F_k^2}}{\sum_{i \neq k}^n \frac{1}{F_i^2}}. \quad (4.2)$$

## 4.2 Additional rule to optimize the threshold values

*Idle Machine does not Bid (IMB)*: Equation 3.17 offers a threshold update rule for idle agents in order to encourage them to bid for tasks of any type. This update rule decreases all threshold values by a value that exponentially increases in time. The idea is that a machine may stay idle for same time rather than being forced to take any task immediately. We observed that this can cause agents to stay idle for very long and therefore has a negative effect on several performance measures. We propose a new update rule, which is employed in case an idle agent refuses to bid for a task it is offered:

$$\theta_{k,c_j} \rightarrow \theta_{k,c_j} - \gamma. \quad (4.3)$$

In this case, the corresponding threshold  $\theta_{k,c_j}$  of the refused task of type  $c_j$  is decreased by the fixed value  $\gamma$ . Variations of  $\theta_{k,c_j}$  takes place within the bounds  $\theta_{min}$  and  $\theta_{max}$ .

## 4.3 Example

In this section we present an example that shows the plasticity of *ATA* to the dynamic changes on the  $DTA_{Hom}$  problem environment. In the paper of Cicirello *et al.* a very similar situation is presented where the adaptation process to the environmental changes takes more than one third of the experimental time. We will show using *ATA* that this process is very quick. We think that the proposed improvement rules are essential to achieve this behavior.

In order to show this, we consider a simple problem instance with 4 identical agents. Each agent has a queue size of 5 trucks. To paint a truck a booth requires 5 time steps. Another 10 time steps are needed for a setup. Trucks exit the assembly line during 420 time steps. If one step is equal to a minute, trucks enter in the system during seven hours. The number of trucks to be painted is in average equal to 336. This number is chosen because it is in the given time the maximum number of trucks that 4 booths can paint considering the process time, no setups and no idle states. The number of trucks that exit the assembly line

is equally distributed during the 420 time steps. In this example trucks can be painted in two colors only: type 1 and type 2. In order to analyze the plasticity capability of the system, we chose a particular color probability mix: for the first 210 time steps the tasks of type 1 appear three times more frequently than those of type 2. Afterwards, these probabilities swap so that the type of task that appeared more frequently appears more rarely. We refer to this probability mix as CHANGE. The parameter set used for *ATA* is the same as those used in Section 6.1.3 for the  $DTA_{Hom}$  problem instances.

For this example we expect that for the first half of the experiment a higher number of agents becomes specialized in task 1 and that this swaps for the second half. Figure 4.3 shows a typical *ATA* behavior on this configuration. At the beginning agents that are in the same starting conditions become specialized and start performing the tasks. From the time step 210 the demand of type 2 tasks becomes high and the relative stimulus increases (Figure 4.3(a)). At the same time, agents working on type 1 tasks wait for more tasks of the same type but none becomes available. Initially these agents do not bid for type 2 tasks. Until here the behavior of the agents of *ATA* is similar to the agents of *R-WASP*. Then, in *ATA* the *IMB* rule takes effect and decreases the threshold of each agent that prefers to rest idle and not bid for type 2 tasks. The effect of the stimulus increment and of the *IMB* rule is that two agents become specialized for type 2 tasks (Figure 4.3(d) and (e)). The others agents do not change their specialization level. This behavior do not change until the end of the experiment.

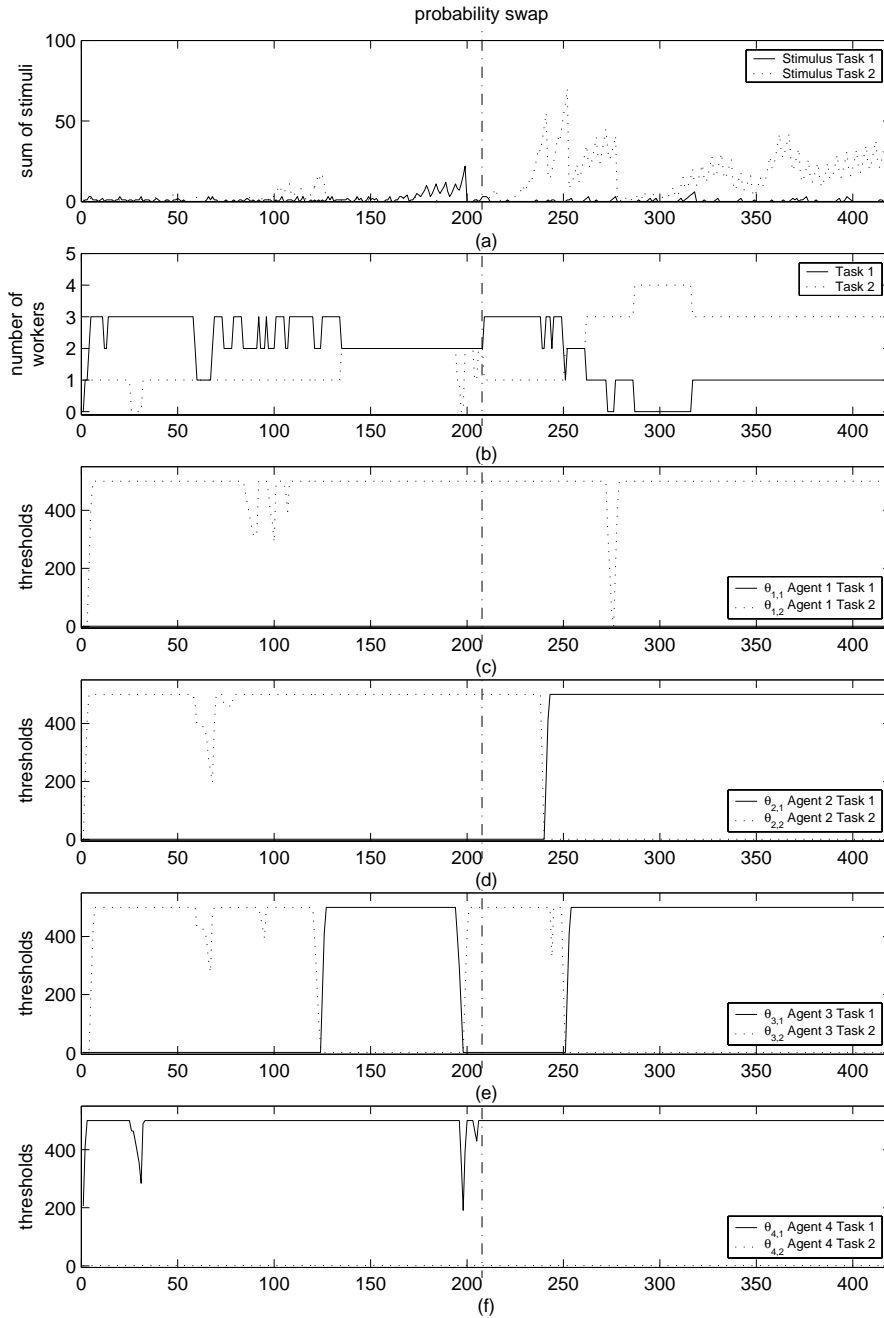


Figure 4.3: The graphs show the sums of the tasks stimuli, the number of working agents for each type of task and the dynamic of thresholds of each agent. Graphs (c), (d) and (e) show that for the first half of the experiment agents 1, 2 and partially 3 are specialized on tasks of type 1 (low thresholds). This behavior is confirmed by graph (b). Graph (f) shows that agent 4 becomes specialized on tasks of type 2. At time 210 the probability mix reverse. Agents still remain specialized to the previous mix. The stimulus of type 2 tasks increases (a) and the agents remain idle. At time 250 (graph (d) and (e)) agents 2 and 3 adapt themselves to the new environment. From this moment to the end of the experiment there are three agents working on tasks of type 2 and one on tasks of type 1 (b).



# Chapter 5

## Extension of the algorithms to the heterogeneous case

The *DTA* problem definition considers agents that can have different processing times for different task types. The insect-based algorithms presented give satisfying results on the homogeneous case of the *DTA* problem but if they are applied on the heterogeneous case the performances are not so acceptable. The problem is that agents bid for a task considering only their specialization level, without taking into account their own characteristics, that is, their capacity to process a task quickly or slowly. In order to have better results, we extend the algorithms so that the faster an agent can perform a task, the higher is the probability to bid for it. In Section 5.1 we present this extension that is applied to the presented insect-based algorithms and is inspired by the caste subdivision of labor observed in social insects. Afterwards, in Section 5.2 we show its impact by discussing an example.

### 5.1 Different process speed (DPS) rule

In an insect colony different castes of agents have a different response to a considered task. Wilson [30] observed a division of labor between insect casts studying ant species *Pheidole*. In normal conditions some castes have higher probability of obtaining a task than others. If in the environment there is a high demand to perform a particular task or a subset of castes is eliminated from the environment, the behavior of the ants in the system changes so that they start to perform tasks for which they are not predisposed. To reproduce this behavior in the considered insect-based algorithms, we introduce the process speed that an agent  $k$  has for a task  $j$  of type  $c_j$  in the probability function  $P(s_j, \theta_{k,c_j})$ . The most promising probability function is obtained modifying Equation 3.14 as follow:

$$P(s_j, \theta_{k,c_j}) = \frac{s_j^2}{s_j^2 + \theta_{k,c_j}^2 * (t_{proc,k,c_j} - tmin_{proc,c_j} + 1)}, \quad (5.1)$$

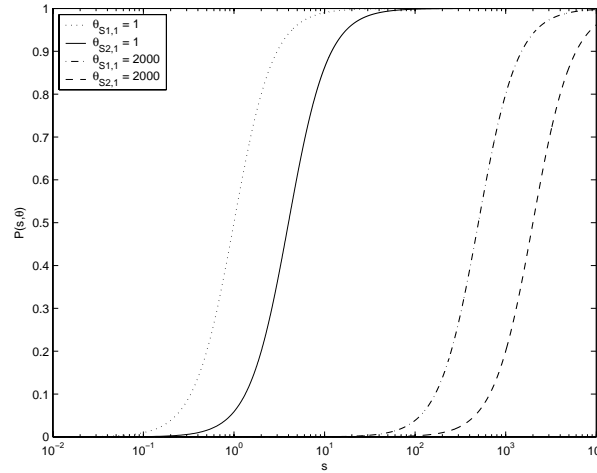


Figure 5.1: The threshold response function that one agent of subset S1 and one agent of subset S2 have for a task of type 1 with different specialization levels.

where  $t_{proc,k,j}$  is the processing time that agent  $k$  has for task  $j$  and  $t_{min_{proc},c_j}$  is the minimum processing time in the system for the type of task  $c_j$ . The added term performs like a weight to the specialization level during the bidding process.

We study the probability function in a simple instance of the *DTA* problem where there are two sets of working agents with two booths for each set and two types of task. The process time is given in Table 5.1(a) whereas the relative probability function  $P(s_j, \theta_{k,c_j})$  is presented in Figure 5.1. The figure shows that agents of subset S1 always have a higher probability to bid for tasks of type 1 than agents of subset S2. An important characteristic of this function is that the distance between the response to a stimulus of an agent  $k$  of the first subset and the same response by an agent of the second set is constant and independent from the specialization value  $\theta_{k,c_j}$ . This improvement allows a correct distribution of work between agents with a behavior that still maintains a high plasticity level to the environmental changes. When an insect-based algorithm uses the *DPS* rule, we refer to it with a letter  $c$  at the end of the respective name (*ABAc*, *R-WASPC*, *ATAc*). Finally, we observe that, if we use these extended algorithms on a *DTA<sub>Hom</sub>* problem instance, they perform as the original ones.

## 5.2 Example

The aim of this example is to analyze the division of labor among agents of a *DTA* instance using *ATAc* algorithm. We consider a situation where there is an asymmetric demand of types of tasks. The considered instance has 2 subsets of working agents (S1 and S2) with 2 booths within each subset. Trucks can be



Table 5.1: Values for a *DTA* problem instance with two subsets of working agents, two agents for each subset and two different types of tasks.

(a) Process time matrix.			(b) Number of worked tasks.		
	Type 1	Type 2		Type 1	Type 2
subset S1	3	9	subset S1	278	0
subset S2	9	3	subset S2	30	138

painted in two colors: type 1 and type 2. Each agent has a queue size of 5 trucks. 10 time steps are needed for a reconfiguration. Trucks exit the assembly line during 420 minutes. Process times are described in Table 5.1(a). The number of trucks to be painted is on average equal to 446. This number is the maximum number of trucks paintable in 420 minutes by the system considering that three booths work for one type of task, the fourth one works on the other type of task and no setups and idle times are necessary. The color probability mix is asymmetric with a higher number of type 1 tasks: a truck of type 1 has probability 0.77619 to appear at each time step and a truck of type 2 has probability 0.332. We refer to this probability mix as DIFF. The parameter set used by *ATAc* is the same as that used in Section 6.1.3 for the *DTA* problem instances.

Before running the example we expect this behavior:

- In a normal condition tasks are executed by agents that need short time to process them.
- If there is a high demand of a type of tasks and there are no more agents that perform it quickly, agents that perform it slowly start working for it.
- If an agent that performs a type of task quickly and an other agent that performs the same type slowly are both specialized for that type, the quicker agent should have a higher probability to process it.

Figure 5.2 shows a typical *ATAc* behavior on this particular *DTA* problem instance. At the beginning of the experiment agent 1 and 2 within subset S1 start to perform type 1 tasks and become specialized on it (Figure 5.2(b), times 0-150). Instead, agent 3 and 4 within subset S2 that are able to perform type 2 tasks quickly, become specialized on that type (Figure 5.2(c)).

The asymmetric probability mix at time 100 increases the demand of type 1 tasks (Figure 5.2(a)) but in the system all the agents of subset S1 are busy so at time 150 the high stimulus of type 1 leads agent 4 of the subset S2 to work on type 1 tasks (Figure 5.2(g), time 150). From time step 150 agent 4 becomes specialized in tasks of type 1. In fact, its threshold for that type of task is close to 0 (Figure 5.2(g), time 150-end). Agent 3 still works on tasks of type 2. In fact,

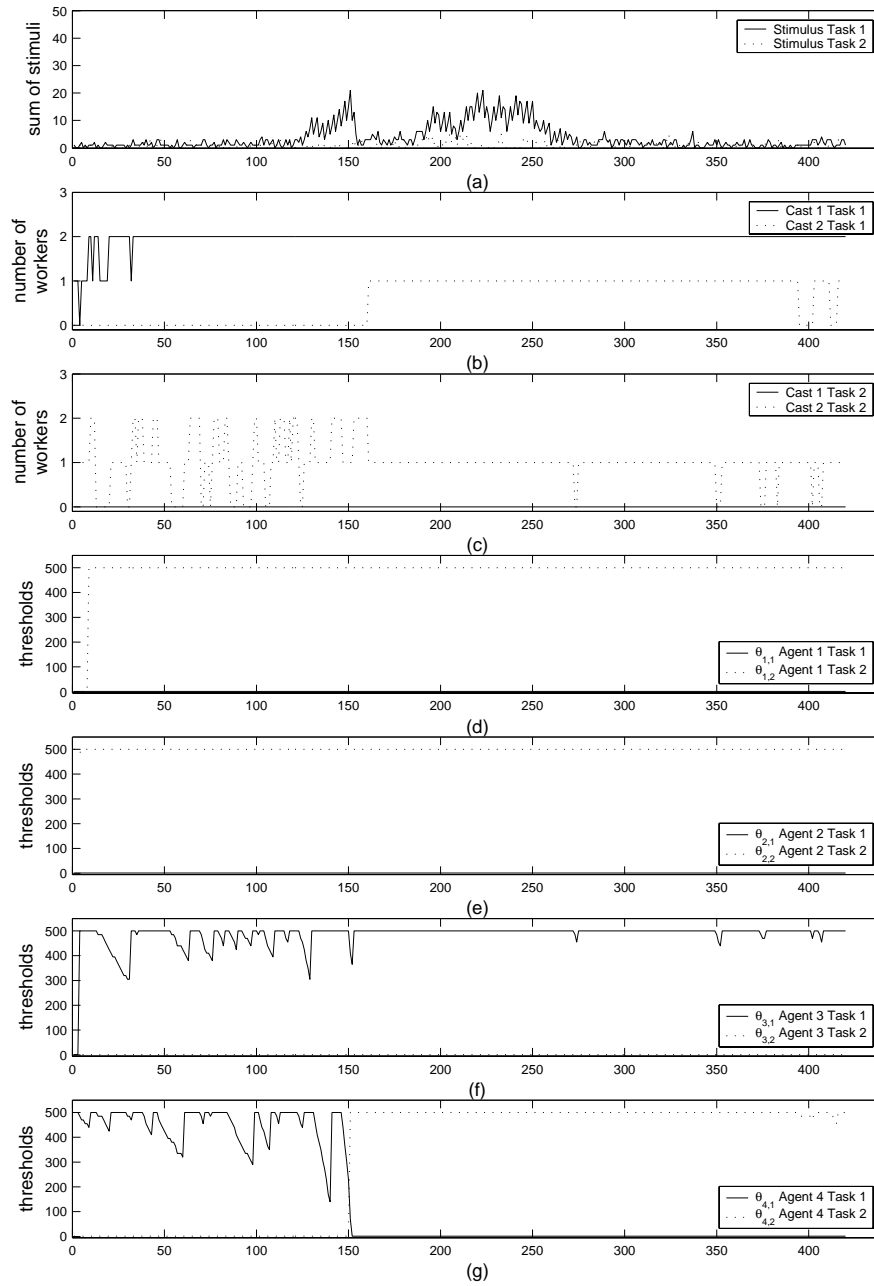


Figure 5.2: The graphs show the tasks stimuli, the number of working agents for each type of task and the dynamics of the threshold values of each agent. At the beginning of the experiment only agents 1 and 2 work on type 1 tasks (Figure (b)), and only agents 3 and 4 on type 2 (Figure (c)). Type 1 stimuli increases from time 100 to 150 (Figure (a)) until when the agent 4 (Figure (g)) starts to work on this type. From time 150 to the end of the experiment type 1 stimuli become low (Figure (a)). From this time on, all the agents of the subset S1 (Figure (b)) and one agent of the subset S2 work for tasks of type 1. Agent 3 is enough to satisfy the low demand of type 2 tasks.

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its threshold value for that type of task is close to 0 (Figure 5.2(f), time 0-end). Table 5.1(b) represents the number of worked tasks at the end of the experiment and confirms that type 1 tasks are performed principally by subset S1 and type 2 tasks by subset S2, that is, agents that are able to perform tasks quickly, using the DPS rule, really process them.



# Chapter 6

## Empirical analysis

Previous works on the homogeneous case of the *DTA* problem [6, 7, 19] analyze few and sometimes simple instances of the problem where it is difficult to show that an algorithm performs better than another one. It is possible that a simple modification of the instance leads to a drastic performance decrease. Moreover, little or no analysis has been done to show the contribution of the proposed rules.

The aim of this chapter is to compare all the presented algorithms on the *DTA* problem and analyze the influence of each presented rule on the makespan.

We have introduced two types of rules with the objectives to:

1. improve the algorithm of Cicirello *et al.* to particularly dynamic  $DTA_{Hom}$  problem instances.
2. extend all the insect-based algorithms with the DPS rule to improve the performance on *DTA* problem instances.

According to this, we present two experiments: one that uses a class of instances of the homogeneous problem and another one that uses a class of instances of the heterogeneous problem.

In the following section we describe the instance generators, a summary of the algorithms we use in the experiments and the methodology to tune their parameters. Afterwards, Section 6.2 describes the obtained results.

### 6.1 Setup

A lot of work has been done to make a strict configuration and evaluation of the experiments. First of all in our experiments we consider *classes of instances* of the problem. A class contains problem instances that differ by variables such as the number of working agents, the task types and the color probability mix. In this section we define two problem classes in order to describe two real-world painting environments. Afterwards, for each considered algorithm we present the

Table 6.1: Summary of the classes of instances of the  $DTA$  and  $DTA_{Hom}$  problem considered in the experiments.

	$DTA_{Hom}$ Class	$DTA$ Class
Subsets of agents	1	2
Max. number of agents	24	12
Broken probability	0.02	0.02
Queue length	10	5
Process Time	5	3-9
Setup Time	10	10
Simulation Time	420	420
Number of Tasks	2016	840
Avg. types of tasks	12	10
Types mixes	1) $P(1..n/4) = 3P(n + 1/4..n)$ 2) like 1, switch after 210 steps	1) $P(1..n/2) = 3P(n + 1/2..n)$ 2) like 1, switch after 210 steps
Probability between mixes	0.5	0.5

best combination of the parameter values tuned by an Evolutionary Algorithm (EA). Moreover, we summarize all the algorithms we use in the experiments and we introduce a simple, non-adaptive algorithm in order to emphasize during the results analysis the differences between adaptive and non-adaptive systems.

### 6.1.1 Instance generators

An instance generator is a tool able to generate various instances from a class of the problem. We consider two instance generators able to obtain two classes of instances of the  $DTA$  problem. While the first one creates instances of the homogeneous problem, the second one creates instances of the heterogeneous problem. The first class of instances contains all instances with identical agents. On this class we are able to compare all the presented algorithms and to study the performance of each rule introduced in  $ATA$ . The second class of instances contains two subsets of agents, the first one able to perform quickly half of the types of tasks, while the second one has the opposite behavior. Applying on this class the original algorithms for the  $DTA_{Hom}$  problem and the insect-based algorithms with the DPS rule, we are able to compare the performance of each algorithm and to understand the contribution of the introduced rule. Table 6.1 summarizes the configurations of the two considered classes of instances. Instances within a same class may differ by the number of agents, the number of task types and the type of the probability mix of the tasks. In the following we describe each class separately.

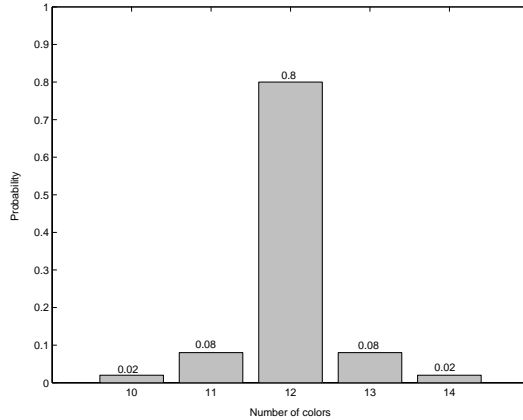


Figure 6.1: Probability distribution of the number of colors for the  $DTA_{Hom}$  experiment.

### $DTA_{Hom}$ class

This class contains all instances of the homogeneous problem where the agents are identical. In this class we try to simulate a typical working day of a big painting factory. According to this, the experimental time is equal to 420 minutes, that is, 7 working hours. The agents are 24 identical painting booths. In order to simulate the possibility to have some booths broken we introduce a variability on the number of maximum booths each instance has. We refer this variability to as broken probability. The broken probability for this class of the problem is equal to 0.02. Here the agents have a queue size equal to 10. The process time of each booth is equal to 5 minutes, 10 minutes are needed for a reconfiguration.

The number of trucks that exit the assembly line is equal to 2016 and is independent of the number of agents. This number is chosen because it is the maximum number of trucks that 24 booths can paint considering the process time, no setups and no idle time.

For this class we extract the number of colors from the probability distribution presented in Figure 6.1. Color types are assigned to the trucks according to the two mixes:

1. A part of the  $n$  colors have an higher probability than the others:

$$\begin{cases} \sum_{i=1}^{\lfloor n/4 \rfloor} P(i) = 3 \sum_{j=\lfloor n/4 \rfloor + 1}^n P(j) \\ P(1) = \dots = P(\lfloor n/4 \rfloor) \\ P(\lfloor n/4 \rfloor + 1) = \dots = P(n) \end{cases}$$

2. like the previous one, but after 210 minutes types that appear more frequently appear more rarely and vice versa.

Each instance uses with the same probability one mix or the other.

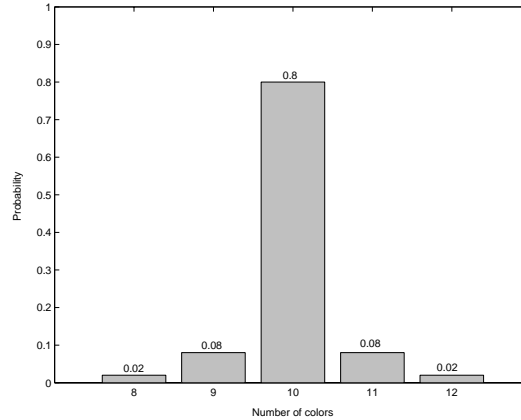


Figure 6.2: Probability distribution of the number of colors for the *DTA* experiment.

### *DTA* class

This class contains instances of the heterogeneous problem where the agents differ by their processing speed. In this class we try to simulate a typical working day of a medium painting factory. Trucks exit from the assembly line for 420 minutes. We consider 12 painting booths with a probability of being broken that is equal to 0.02. Each agent has a queue size equal to 5. In this case there are two subsets of agents: one needs 3 minutes to process the first half of the available types of tasks and 9 minutes for the other half instead the other subset has the opposite behavior. For both the subsets the setup time is equal to 10 minutes.

The number of trucks exiting the assembly line is always equal to 840, which is the maximum number of trucks that 12 booths can paint considering an average process time of 6 minutes, no setups and no idle time.

For this class we extract the number of colors from the probability distribution presented in Figure 6.2. Color types are assigned to the trucks according to the two mixes:

1. A part of the  $n$  colors have an higher probability than the others:

$$\begin{cases} \sum_{i=1}^{\lfloor n/2 \rfloor} P(i) = 3 \sum_{j=\lfloor n/2 \rfloor + 1}^n P(j) \\ P(1) = \dots = P(\lfloor n/2 \rfloor) \\ P(\lfloor n/2 \rfloor + 1) = \dots = P(n) \end{cases}$$

2. like the previous one, but after 210 minutes types that appear more frequently appear more rarely and vice versa.

Each instance uses with the same probability one mix or the other.



Table 6.2: Summary of the algorithms applied in both the experiments.

$DTA_{Hom}$ Class	$DTA$ Class	
<i>MBA</i>	<i>MBA</i>	-
<i>ABA</i>	<i>ABA</i>	<i>ABAc</i>
<i>LOCUST</i>	<i>LOCUST</i>	-
<i>R-WASP</i>	<i>R-WASP</i>	<i>R-WASPC</i>
<i>ATA</i>	<i>ATA</i>	<i>ATAc</i>

### 6.1.2 Algorithms summary

Table 6.2 summarize all the algorithms we use during the empirical analysis. We consider a class of instances of the homogeneous ( $DTA_{Hom}$ ) problem and a class of the heterogeneous ( $DTA$ ) problem. We run on the  $DTA_{Hom}$  problem instances the market-based algorithm *MBA* of Morley described in Section 3.1.1, the insect-based algorithm *ABA* of Campos *et al.* described in Section 3.2.1, the insect-based algorithm *R-WASP* of Cicirello *et al.* described in Section 3.2.2 and our proposed algorithm *ATA* described in Section 4. For the  $DTA$  problem we run all the original algorithms and the three insect-based algorithms with the DPS rule.

In the following we present *LOCUST*, a dummy, non-adaptive algorithm used as a base-line for evaluating the performances of the presented algorithms. In both the experiments we apply also this algorithm in order to have a comparison between adaptive and non-adaptive systems. *LOCUST* has functionalities inspired by the presented algorithms but it does not consider the specialization of each agent. It is described in the following.

#### The *LOCUST* algorithm

In this algorithm agents are independent units that autonomously bid to obtain tasks using a force value which is obtained by the sum of the time the agent needs to finish the working task plus the sum of processing times of each task in its queue and the current task plus the possible setup times between each queued task. At each time step agents bid to obtain tasks if their queue are not full. The agent with the lower force is assigned the task at the end of its queue. If two or more agents have the same force, the winner is chosen randomly. If no agents bid for a task, the task remains in the storage. For this simple algorithm no parameter tuning is necessary.

### 6.1.3 Parameters tuning

The aim of the tuning is to find a good set of parameter values for each algorithm. We apply the tuning for all the algorithms considered in this thesis because each one has some parameters to determine. In the *MBA* algorithm we tune the three constants in Equation 3.1. In the *ABA* algorithm we tune the constants  $\alpha$  and  $\beta$  of Equation 3.11 and the two constants used in the update rules. In the *R-WASP* algorithm we tune the constants presented in the three update rules and in the *ATA* algorithm the same constants of *R-WASP* plus the one for the new *IMB* rule. For the insect-based algorithms we fix the range of the thresholds to  $\theta_{min} = 1$  and  $\theta_{max} = 500$ . The initial threshold  $\theta_{init}$  is fixed to 1.

Table 6.3 describes for each algorithm used in this experiment which parameters are tuned, the relative range and the values found. To tune the parameters of the algorithms we use an Evolutionary Algorithm (EA). The evaluation has been done as follows: we define a *cost function*, that in our case is the makespan to be minimized. Each population of the EA is composed by 20 individuals. An individual represents a set of values of the parameters to be tuned. Each individual is evaluated on 40 instances of the considered problem class and the average of the makespan values is its cost value. For each instance we execute a single run of the algorithm to be tuned. Individuals of a population are evaluated on the same 40 instances of the considered class. In this tuning we stop after 40 generations because normally after 15 generation the cost function becomes stable. Between generations the instances are changed to avoid using not representative instances of the class. Additionally, the tuning considers the elitism between generations so that the best 4 individuals of the previous generation are used in the new one and the other 16 individuals are generated using a self-adaptive  $(\mu + \lambda)$  evolutionary strategy [26, 1]. If an algorithm is used in both the experiments we apply the parameters tuning twice.

Data show a kind of symmetry in the insect-based algorithms between the increment and the decrement of threshold update factors. It means that the agents become specialized during the experiment. Further information concerning the EA, the tuning logs, the generations values, the best individual of each generation and all the cost function values, are available at the thesis web page with address <http://iridia.ulb.ac.be/~rghizzioli/dta/>.

## 6.2 Results

In this section we present and compare the results obtained by the algorithms in the two sets of experiments: the homogeneous case is presented in Section 6.2.1 and the heterogeneous case is presented in Section 6.2.2. The results are achieved running the algorithms of Table 6.2 on the classes of instances summarized in Table 6.1 using the parameters of Table 6.3 on 1000 problem instances. Our

Table 6.3: Summary of the parameter values for all algorithms used in the empirical analysis for both experiments. In the first column there is the names of the algorithm and the names of the tuned parameters. The second column contains the range for each parameter. The third and the fourth column contain the values tuned by the Evolutionary Algorithm. If a value is equal to 0, this means that for that contest the respective rule is not important.

	Range	$DTA_{Hom}$ Class	$DTA$ Class
<i>MBA</i>			
$P$	(0-100)	46	11
$C$	(0-10000)	7200	5710
$L$	(0-5)	2.78	2.25
<i>ABA</i>			
$\xi$	(0-500)	475	215
$\varphi$	(0-500)	67.5	30
$\alpha$	(0-100)	44.6	78
$\beta$	(0-50)	2	2.5
<i>R-WASP</i>			
$\xi$	(0-500)	345	310
$\varphi$	(0-500)	480	26
$\delta$	(0-500)	490	0
<i>ATA</i>			
$\xi$	(0-500)	165	224
$\varphi$	(0-500)	205	115
$\delta$	(0-500)	1.2	0
$\gamma$	(0-500)	34	0
<i>ABAc</i>			
$\xi$	(0-500)	-	430
$\varphi$	(0-500)	-	450
$\alpha$	(0-100)	-	98
$\beta$	(0-50)	-	2.95
<i>R-WASPC</i>			
$\xi$	(0-500)	-	395
$\varphi$	(0-500)	-	6
$\delta$	(0-500)	-	0.5
<i>ATAc</i>			
$\xi$	(0-500)	-	95
$\varphi$	(0-500)	-	65
$\delta$	(0-500)	-	0
$\gamma$	(0-500)	-	25

Table 6.4: Summary of the makespan values for all the algorithms run on the class of instances of the  $DTA_{Hom}$  problem. The table shows the quantile values, the mean, the minimum and the maximum values achieved by each algorithm. The median values show that  $ATA$  performs better than the other algorithms.  $ATA$ , compared with the other algorithms, is also a stable algorithm because has smaller difference between the 1st and the 3rd quantile. For a graphical view see Figure 6.3. For a statistical analysis see Table 6.5.

	<i>ATA</i>	<i>R-WASP</i>	<i>ABA</i>	<i>LOCUST</i>	<i>MBA</i>
Min.	472.0	588.0	717.0	803.0	464.0
1st Qu.	497.0	749.0	843.8	944.0	484.0
Median	509.0	812.5	887.0	980.0	531.5
Mean	513.4	808.0	895.9	984.1	599.2
3rd Qu.	525.0	864.0	940.3	1017.0	706.0
Max.	699.0	1066.0	1156.0	1217.0	1042.0

main performance measure is the makespan. For completeness and for a better understanding we also present the number of setups per agent and the storage dimension. For each experiment we show the contribution to the makespan given by each introduced rule.

### 6.2.1 $DTA_{Hom}$ class

The homogeneous case of the  $DTA$  problem considers a single set of identical agents. In this case agents should specialize on one type of task in order to minimize the required number of setups. A good distribution of the task types between the agents allows a low makespan. Results about the makespan are shown in Table 6.4 and in Figure 6.3.  $ATA$  achieves the best results because, as we showed, it has a high level of plasticity to the environmental changes. Furthermore, the 1000 makespan values produced by  $ATA$  are very similar and compared with the results obtained by the other algorithms it seems that  $ATA$  is not influenced by the variability between instances in the class. In the next paragraph we show the significance of each rule introduced in  $ATA$ . As can be observed, the algorithm of Campos *et al.* does not obtain good results for this class of instances of the  $DTA_{Hom}$  problem. It is also interesting to show a linear performance improvement in time of the insect-based algorithms. Moreover, the market-based algorithm  $MBA$  reaches good performance for this class of instances.

To be sure of the real significance of the obtained results we apply a Wilcoxon Paired Rank Sum Test as presented in Table 6.5. The values show that different results of the makespan between algorithms are significantly different with a confidence level of 95%.

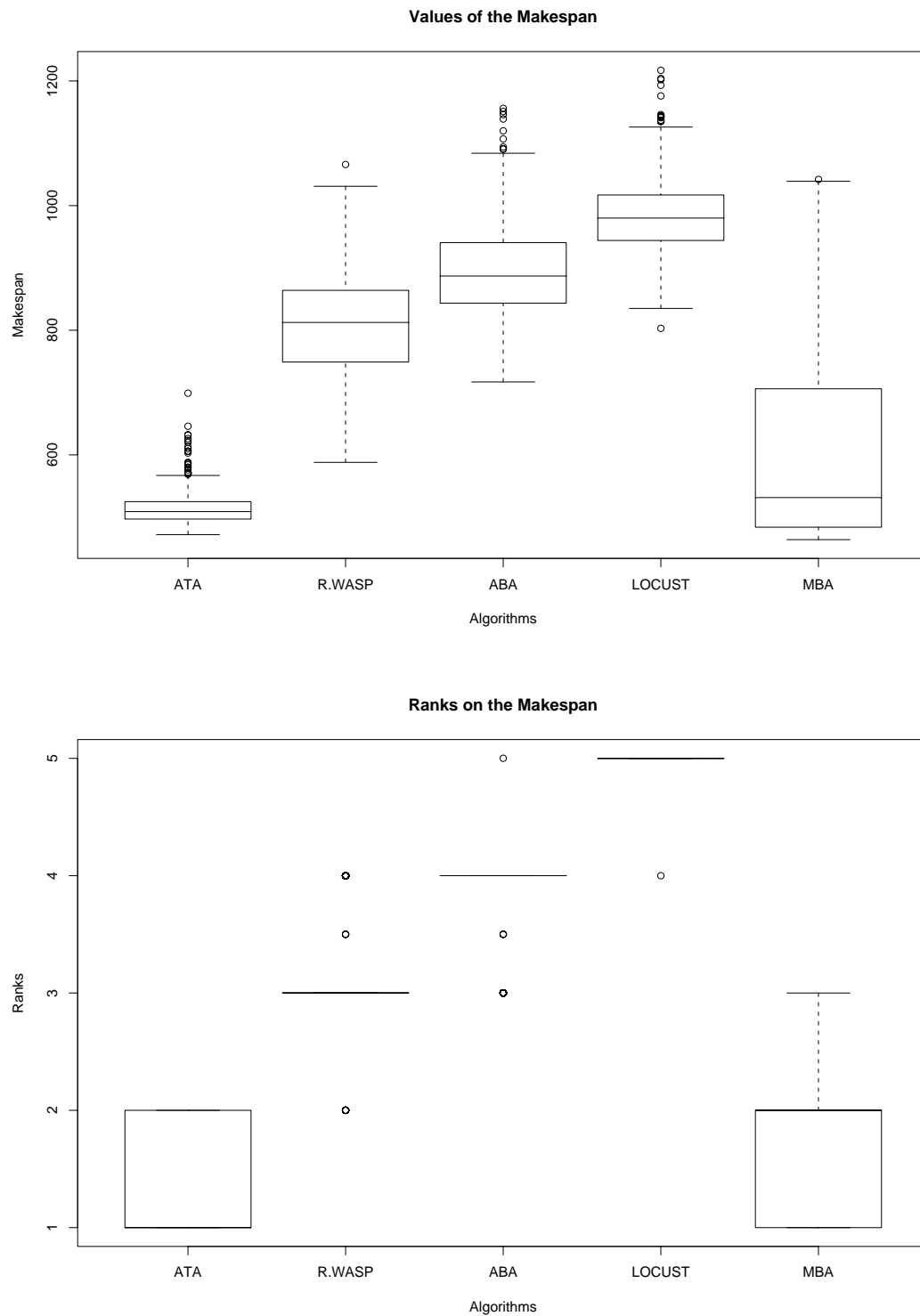


Figure 6.3: Box plot of the values and of the ranks of the makespan for all the algorithms run on the class of instances of the homogeneous problem. *ATA* is the algorithm that has the lower makespan and the smaller quantile representation area.

Table 6.5: Paired Wilcoxon Rank Sum Test applied on the makespan values of the algorithms on the class of instances of the homogeneous problem. Values are obtained with a confidence level of 95%. All results given by this table assure that differences between algorithms on the median values of the makespan are significant.

	<i>ABA</i>	<i>R-WASP</i>	<i>LOCUST</i>	<i>MBA</i>
<i>R-WASP</i>	$< 2.2e^{-16}$	-	-	-
<i>LOCUST</i>	$< 2.2e^{-16}$	$< 2.2e^{-16}$	-	-
<i>MBA</i>	$< 2.2e^{-16}$	$< 2.2e^{-16}$	$< 2.2e^{-16}$	-
<i>ATA</i>	$< 2.2e^{-16}$	$< 2.2e^{-16}$	$< 2.2e^{-16}$	$< 2.2e^{-16}$

Figure 6.4 and Figure 6.5 show the box plot of the number of setups per agent and the storage dimension for each algorithm applied to the  $DTA_{Hom}$  class. These graphs have are similar to the makespan box plot of Figure 6.3. They reconfirm that *ATA* has the best performances also considering the number of setups and storage dimension.

The average number of setups of an agent for the *ATA* algorithm is 3.939 and, on average, 61.47 trucks wait in the storage.

### The significance of the introduced rules for the $DTA_{Hom}$ problem

*ATA* is the solution we propose to solve the homogeneous case of the  $DTA$  problem. *ATA* is an extension of *R-WASP* with all the proposed rules *TUR*, *CFV*, *DOC* and *IMB* activated. Here we perform a statistical analysis to understand the contribution that each rule gives to the makespan.

First of all, as shown in Figure 6.6, we use a binary notation for each possible configuration of *ATA*. For example 0000 indicates that no rules are activated, 1000 only *TUR*, 0100 only *CFV*, 0010 only *DOC*, 0001 only *IMB*, 0110 *CFV* and *DOC*, etc. Makespan data are collected by running all these 16 configurations on 1000 instances on the  $DTA_{Hom}$  problem after a parameter tuning of each of them. The evolutionary algorithm and the methodology used are described in Section 6.1.3. Parameters belonging to unused rules are not tuned.

A first analysis of these data is shown in Figure 6.7(a) and in Figure 6.7(b). Our results show that, on average, configuration 1011 performs better than all the others and that *ATA* is very close to it. Moreover, all possible configurations have a lower makespan than the solution of Cicirello *et al.* (configuration 0000). Figure 6.7(b) shows that results in the right part of the graph, with the *TUR* rule activated, are significantly better than those in the left part of the graph where the rule is deactivated.

Figure 6.8 and Figure 6.9 show the contribution that each rule gives to the

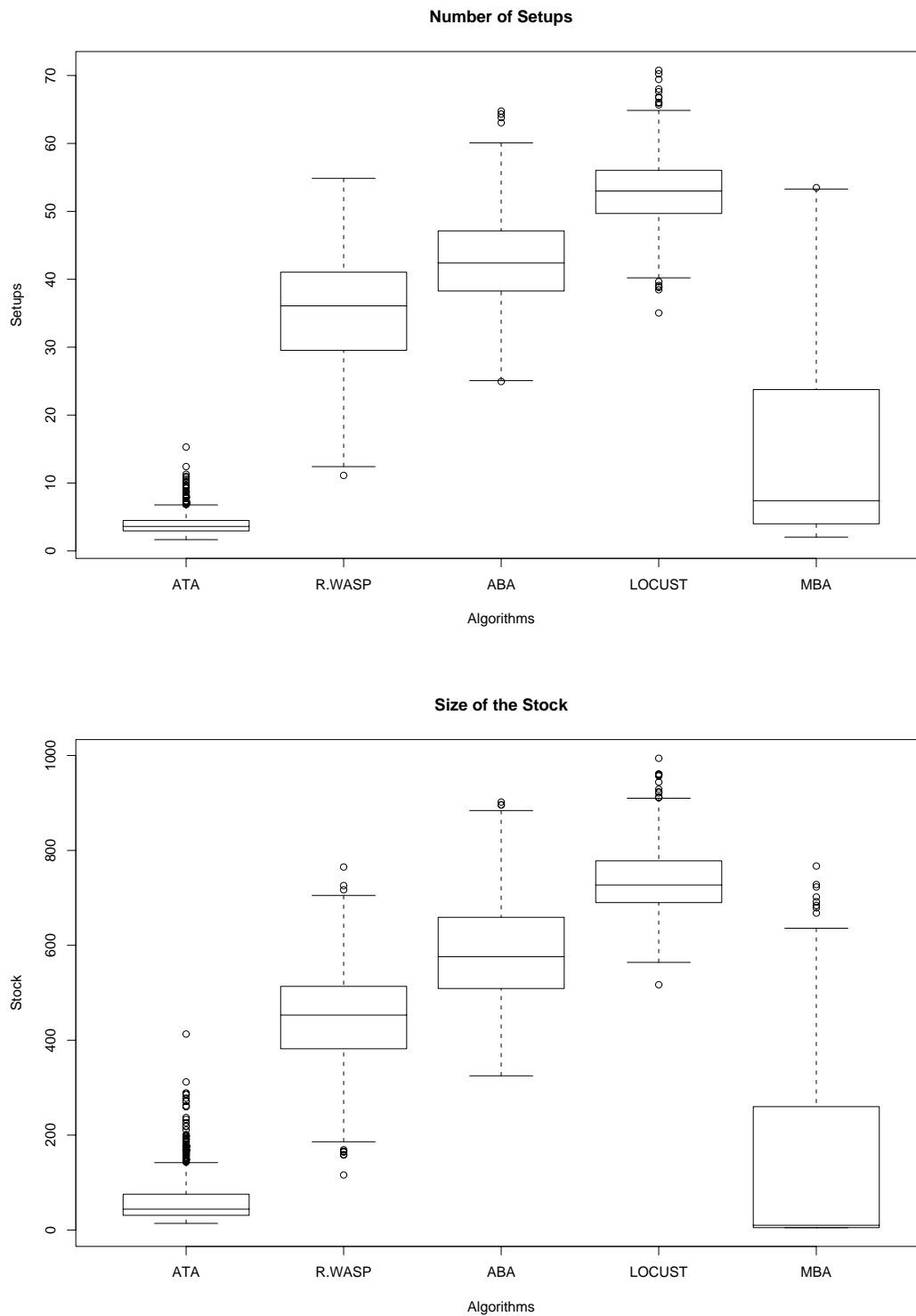


Figure 6.4: Number of setups per agent and storage dimension for the homogeneous experiment. Both figures have a form similar to Figure 6.3. Obviously, a low makespan implies a low number of setups and a low storage usage.

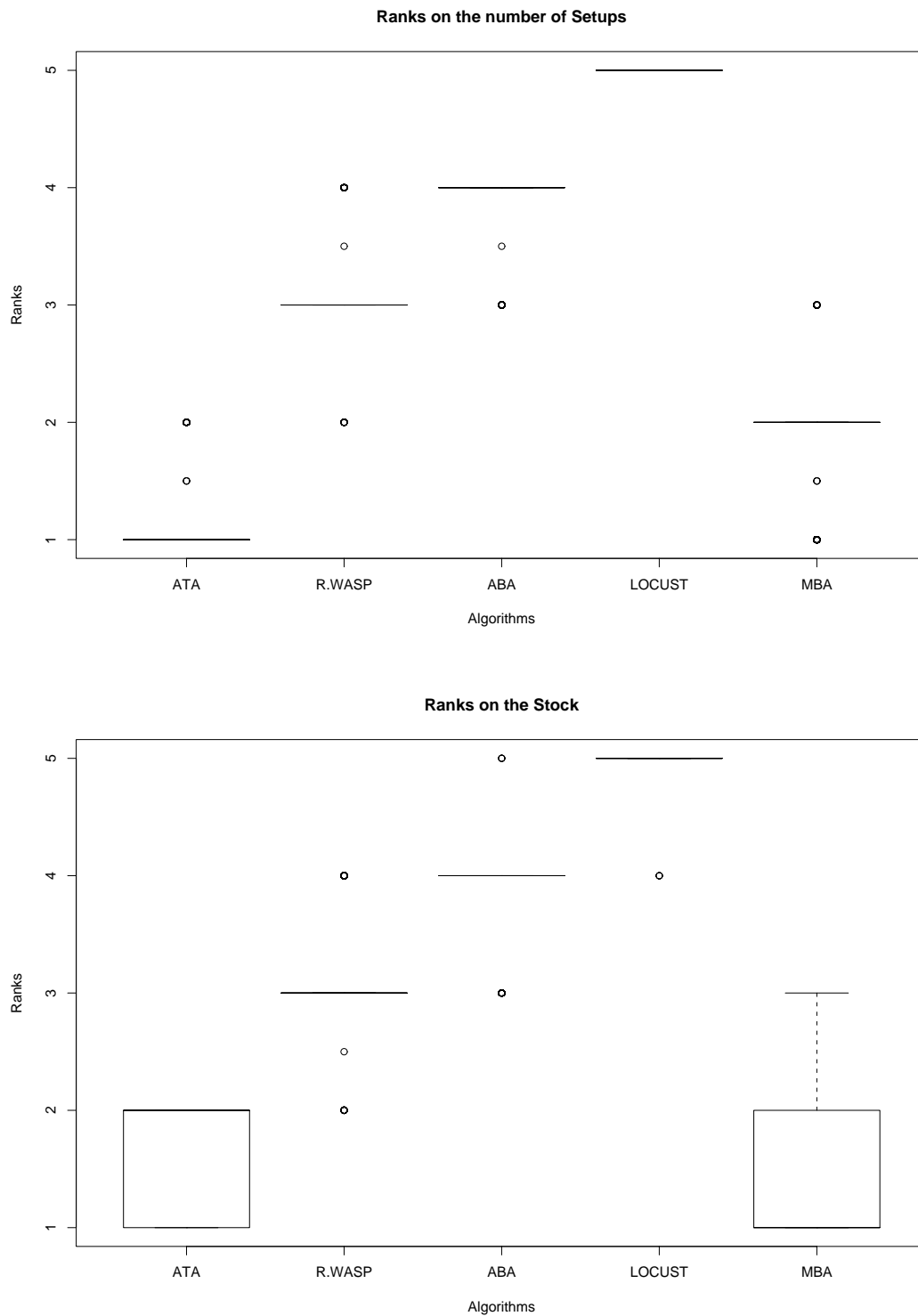


Figure 6.5: Ranks of the number of setups per agent and storage dimension for the  $DTA_{Hom}$  problem.



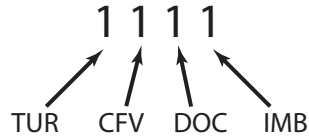


Figure 6.6: Coding system used to indentify the 16 configurations of the proposed algorithm.

Table 6.6: Analysis of variance. The asterisks indicates significance.

	Df	Sum Sq	Mean Sq	$F$ -value	$Pr(> F)$	
TUR	1	4258.2	4258.2	60415.9493	< 2.2e-16	***
CFV	1	0.1	0.1	1.1285	0.2881	
DOC	1	31.3	31.3	444.1618	< 2.2e-16	***
IMB	1	107.5	107.5	1525.5993	< 2.2e-16	***
TUR:CFV	1	9.5	9.5	134.4396	< 2.2e-16	***
TUR:DOC	1	0.001543	0.001543	0.0219	0.8824	
CFV:DOC	1	3.4	3.4	48.7311	3.051e-12	***
TUR:IMB	1	10.9	10.9	155.3420	< 2.2e-16	***
CFV:IMB	1	3.7	3.7	51.7992	6.421e-13	***
DOC:IMB	1	2.4	2.4	34.5107	4.323e-09	***
TUR:CFV:DOC	1	29.5	29.5	418.5021	< 2.2e-16	***
TUR:CFV:IMB	1	3.6	3.6	50.5260	1.226e-12	***
TUR:DOC:IMB	1	2.0	2.0	28.4315	9.839e-08	***
CFV:DOC:IMB	1	16.1	16.1	228.8127	< 2.2e-16	***
TUR:CFV:DOC:IMB	1	2.1	2.1	30.1007	4.164e-08	***
Residuals	15984	1126.6	0.1			

makespan averaged on all configurations where a considered rule is activated independently the other rules. We clearly observe that if *TUR* is activated there is a large difference on the makespan values. Instead, the *CFV* rule does not give any apparent contribution to the results. Finally, *DOC* and *IMB* give similar contribution to the makespan.

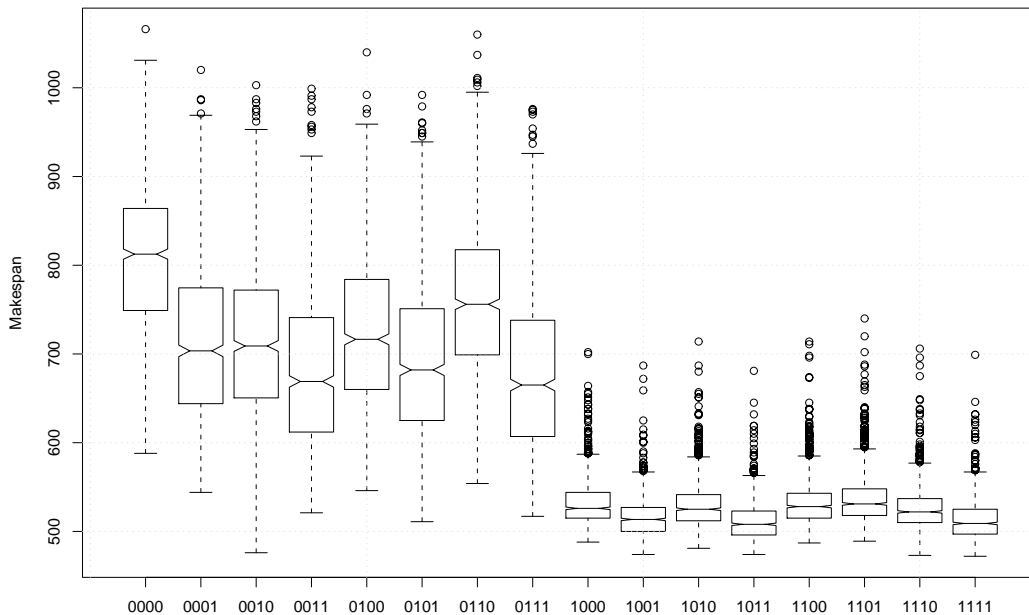
In order to formally assess the contribution of the different rules and their interactions, according to [28], we have considered an ANOVA analysis. As it can be observed in Figure 6.10, the residual of the makespan data does not meet the hypothesis of the ANOVA test, that is, linearity and heteroskedasticity. Therefore, the analysis was not conducted on makespan data but on the following transformation:  $x' = \log(420 - x)$  where  $x$  represents a single makespan result. Figure 6.11 shows that after transforming the makespan values the residuals are reasonably fine.

An ANOVA analysis on this model is show in Table 6.6. The data show that *TUR* gives a large contribution to the makespan while *CFV* does not. Further-

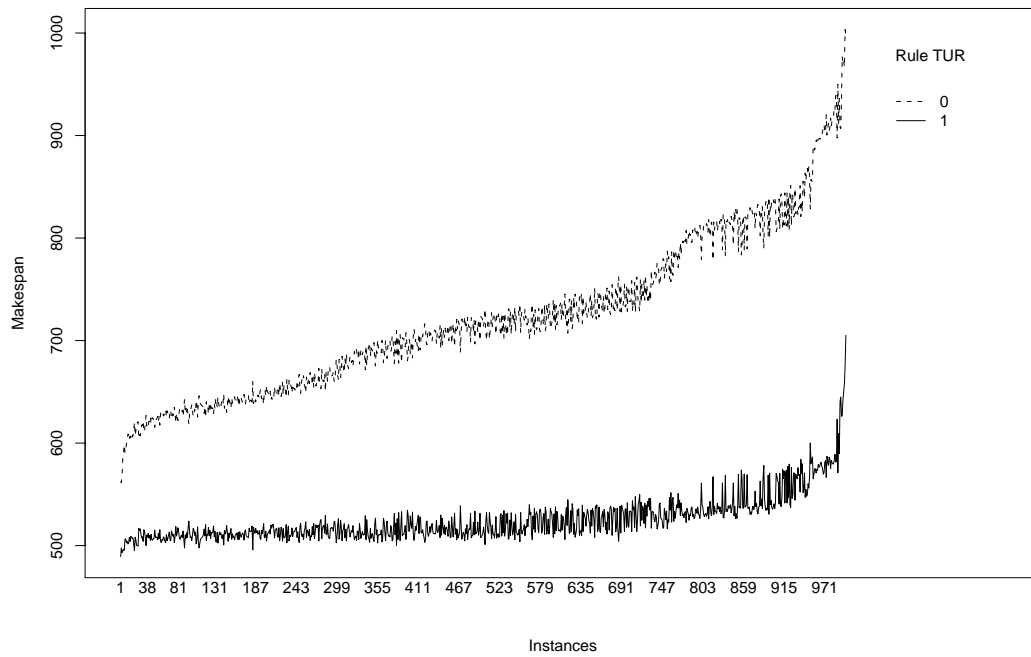
Figure 6.7: Makespan values obtained by each configuration of *ATA* activating and deactivating the proposed rules on the  $DTA_{Hom}$  problem class. For the coding system used to refer to the algorithms see Figure 6.6.

	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
0000	588	749.0	812.5	808.0	864.0	1066
0001	544	644.0	703.5	714.5	774.3	1020
0010	476	650.8	709.0	717.4	772.0	1003
0011	521	612.0	669.0	684.0	741.0	999
0100	546	660.0	716.5	725.3	784.0	1040
0101	511	625.0	682.0	693.4	751.0	992
0110	554	699.0	756.0	760.8	817.3	1060
0111	517	607.0	665.0	678.8	738.0	976
1000	488	515.0	526.0	533.3	544.0	702
1001	474	500.0	513.5	516.1	527.0	687
1010	481	512.0	525.0	530.5	541.3	714
1011	474	496.0	508.0	512.6	523.0	681
1100	487	515.0	528.0	533.4	543.0	714
1101	489	518.0	531.0	537.6	548.0	740
1110	473	510.0	522.0	526.9	537.0	706
1111	472	497.0	509.0	513.4	525.0	699

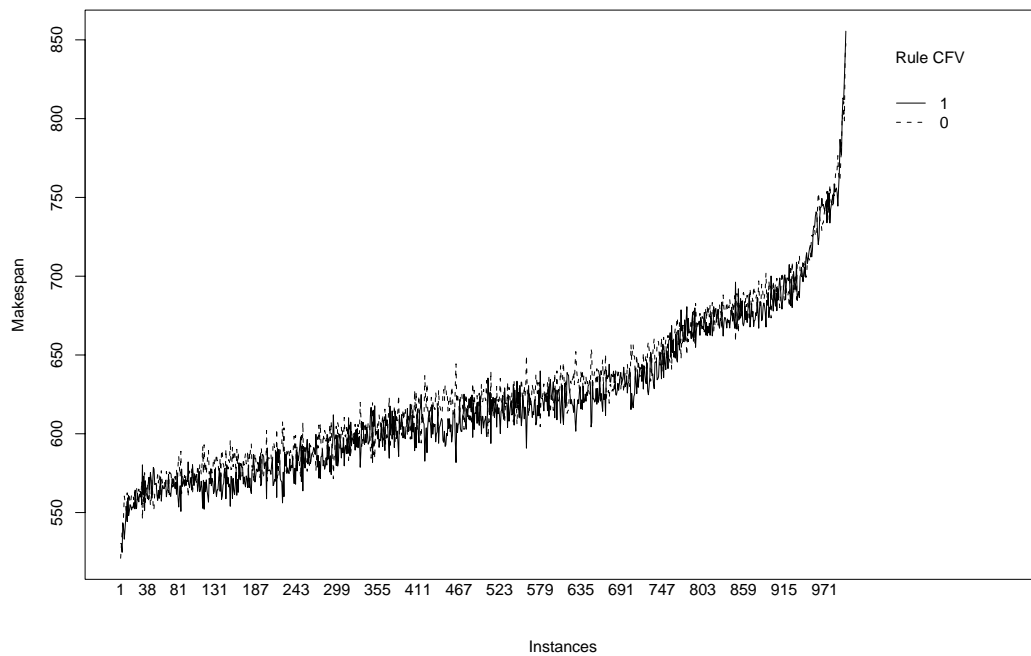
(a)



(b)

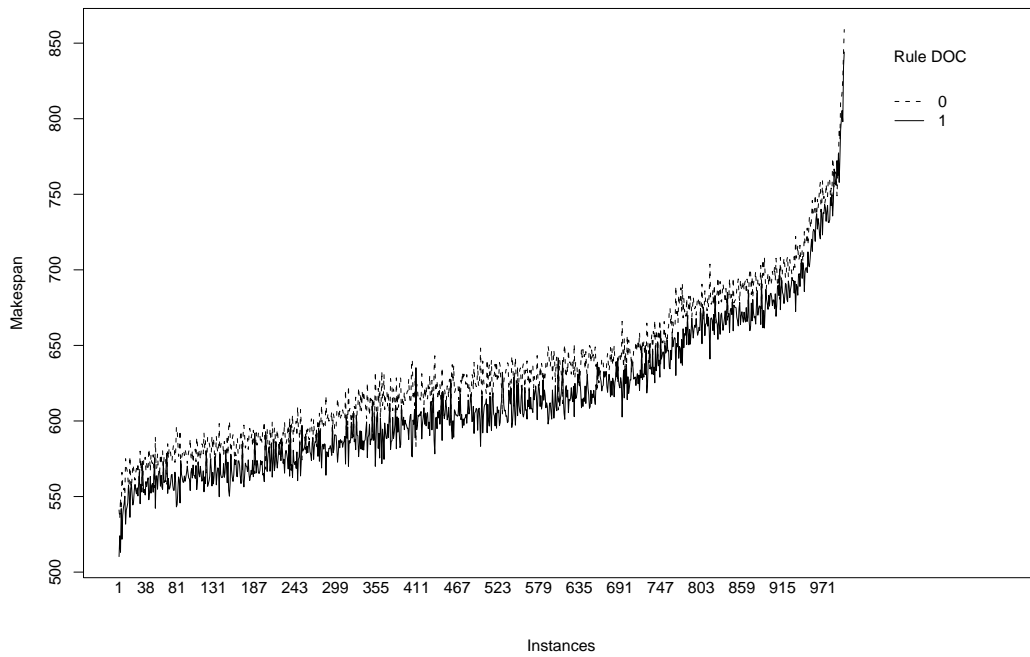


(a)

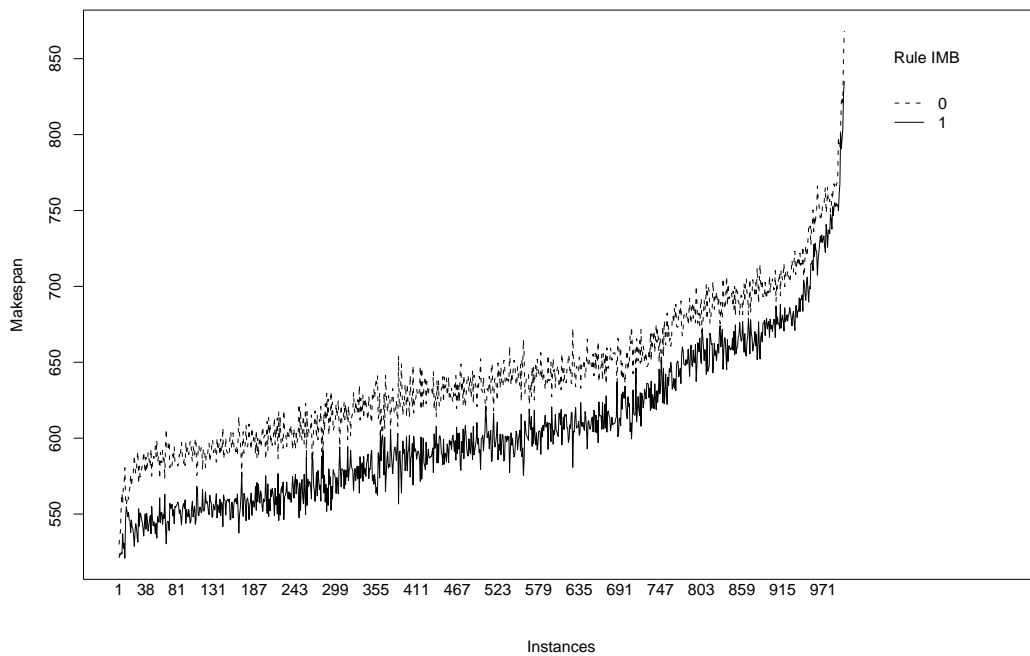


(b)

Figure 6.8: Makespan values on the ranked instances considering the rules *TUR* and *CFV*.

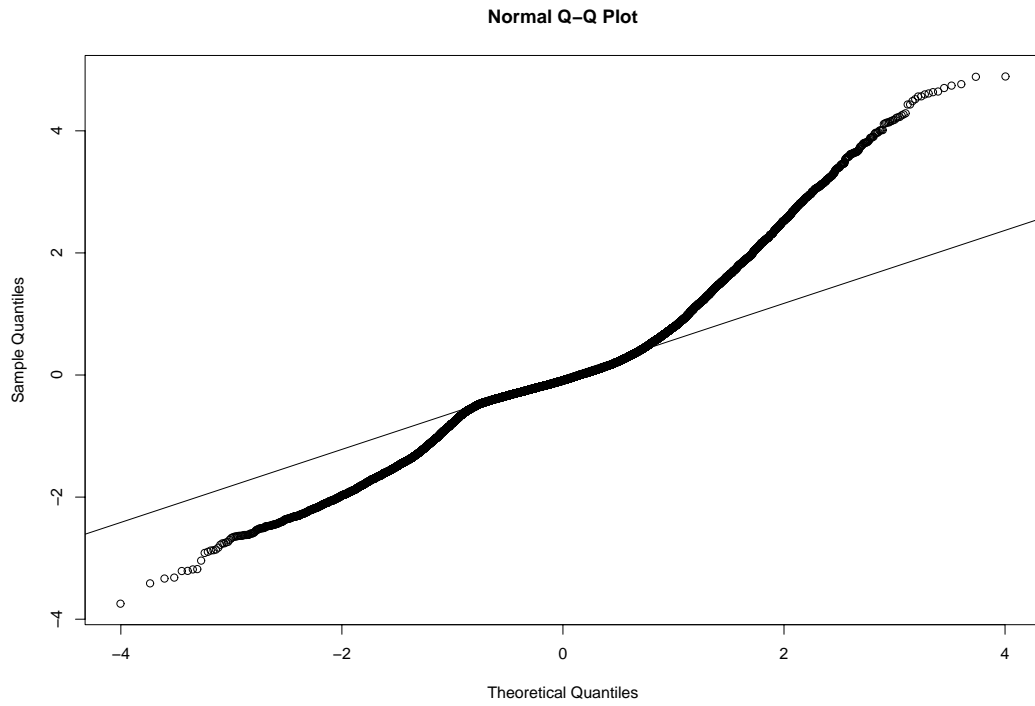


(a)

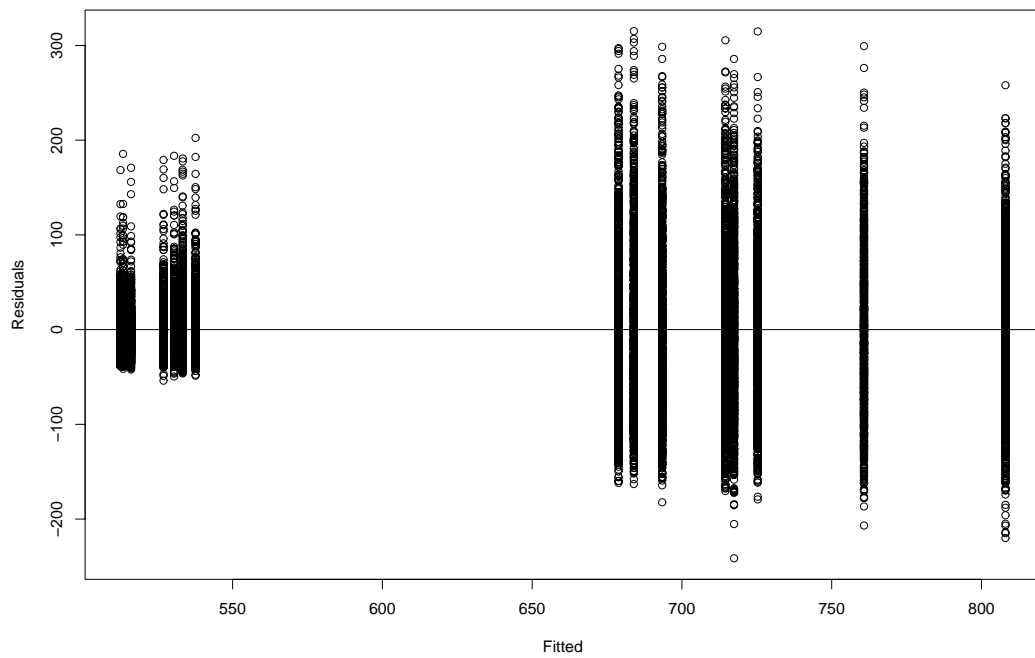


(b)

Figure 6.9: Makespan values on the ranked instances considering the rules *DOC* and *IMB*.

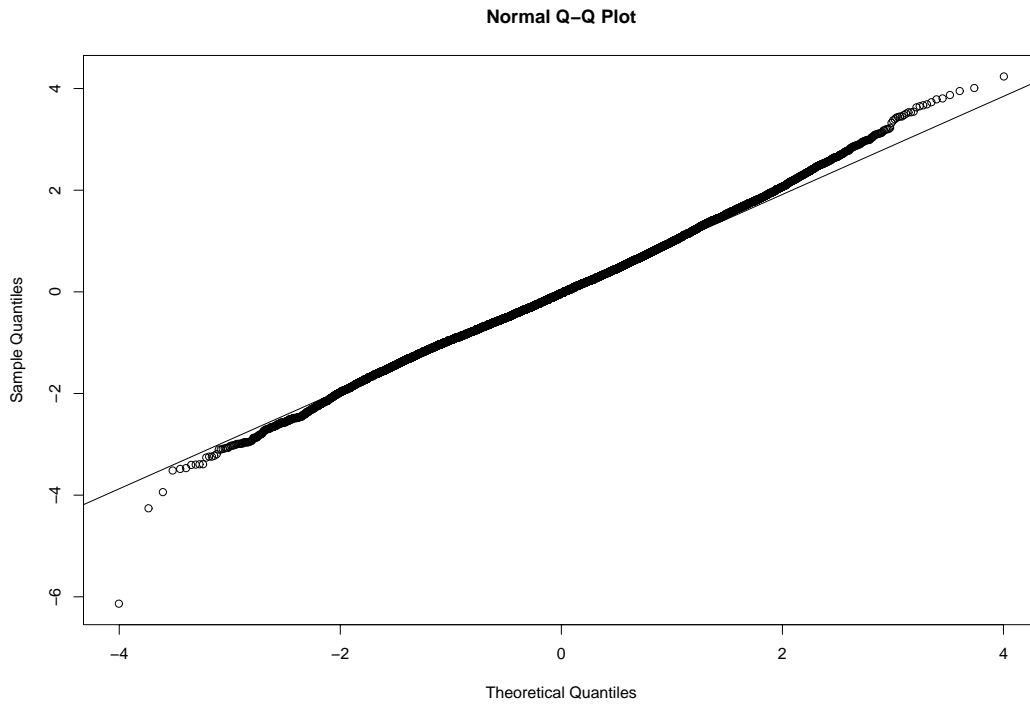


(a)

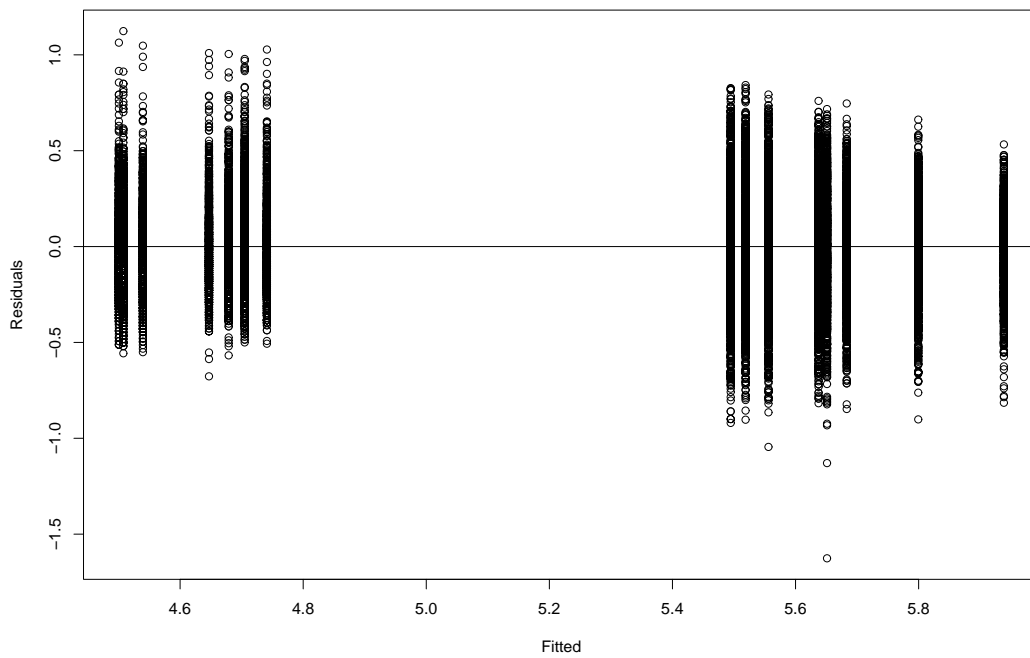


(b)

Figure 6.10: Residual check of the linear model using makespan data.



(a)



(b)

Figure 6.11: Residual check of the linear model using a transformation of the makespan data.

Table 6.7: Summary of the makespan values for all algorithms run on the class of instances of the heterogeneous problem. We compare the original algorithms and the insect-based algorithms with the Different Process Speed (DPS) rule activated. The median values show that algorithms with the DPS rule perform better than the respective algorithms without this rule. Again, *ATA* is the algorithm that has better performance compared with the others original algorithms. For a graphical view of these results see Figure 6.12. For a statistical test on these data we refer to Table 6.8.

	<i>ATA</i>	<i>R-WASP</i>	<i>ABA</i>	<i>LOCUST</i>	<i>MBA</i>	<i>ATA<sub>c</sub></i>	<i>R-WASP<sub>c</sub></i>	<i>ABA<sub>c</sub></i>
Min.	427.0	487.0	428.0	647.0	429.0	428.0	426.0	426.0
1st Qu.	521.0	795.0	884.0	928.0	861.8	471.0	460.0	678.0
Median	548.0	847.0	941.5	952.0	906.0	486.0	506.0	837.0
Mean	557.5	845.6	917.8	959.5	896.4	485.6	525.6	790.7
3rd Qu.	578.0	897.3	979.0	977.3	944.0	499.0	561.0	913.0
Max.	956.0	1273.0	1341.0	1329.0	1321.0	622.0	1018.0	1311.0

more, also *IMB* and *DOC* bring a contribution less important than *TUR* but still significant.

### 6.2.2 DTA class

This experiment considers two subsets of agents: one performs fast in half of the available types of tasks and slow in the second half and the other one vice versa. Agents should bid for tasks that they are able to process quickly. Moreover, they take into account the task type in their queue to minimize the number of setups. If an algorithm achieves this behavior it should obtain a low makespan. A low makespan implies a low number of setups and a low storage usage. In this experiment are compared all the original algorithms presented and the insect-based algorithms with the DPS rule activated. The algorithms used in the previous experiments are applicable to the heterogeneous case of the *DTA* problem. In fact they consider the different process times during the dominance contest. Comparing the algorithms with and without the DPS rule we are able to study its contribution.

Table 6.7 summarizes the makespan values achieved by each algorithm for this class of instances. The respective box plot is presented in Figure 6.12. For this experiment *ATA<sub>c</sub>* obtains the best results concerning the makespan and it is very close to the makespan lower bound (420 minutes). Moreover, we observe that the performance order of the original algorithms is the same as observed in Figure 6.3. Again, we confirm that adaptive algorithms perform better than the non-adaptive algorithm *LOCUST*. Only *MBA* has a worsening of performance. Algorithms

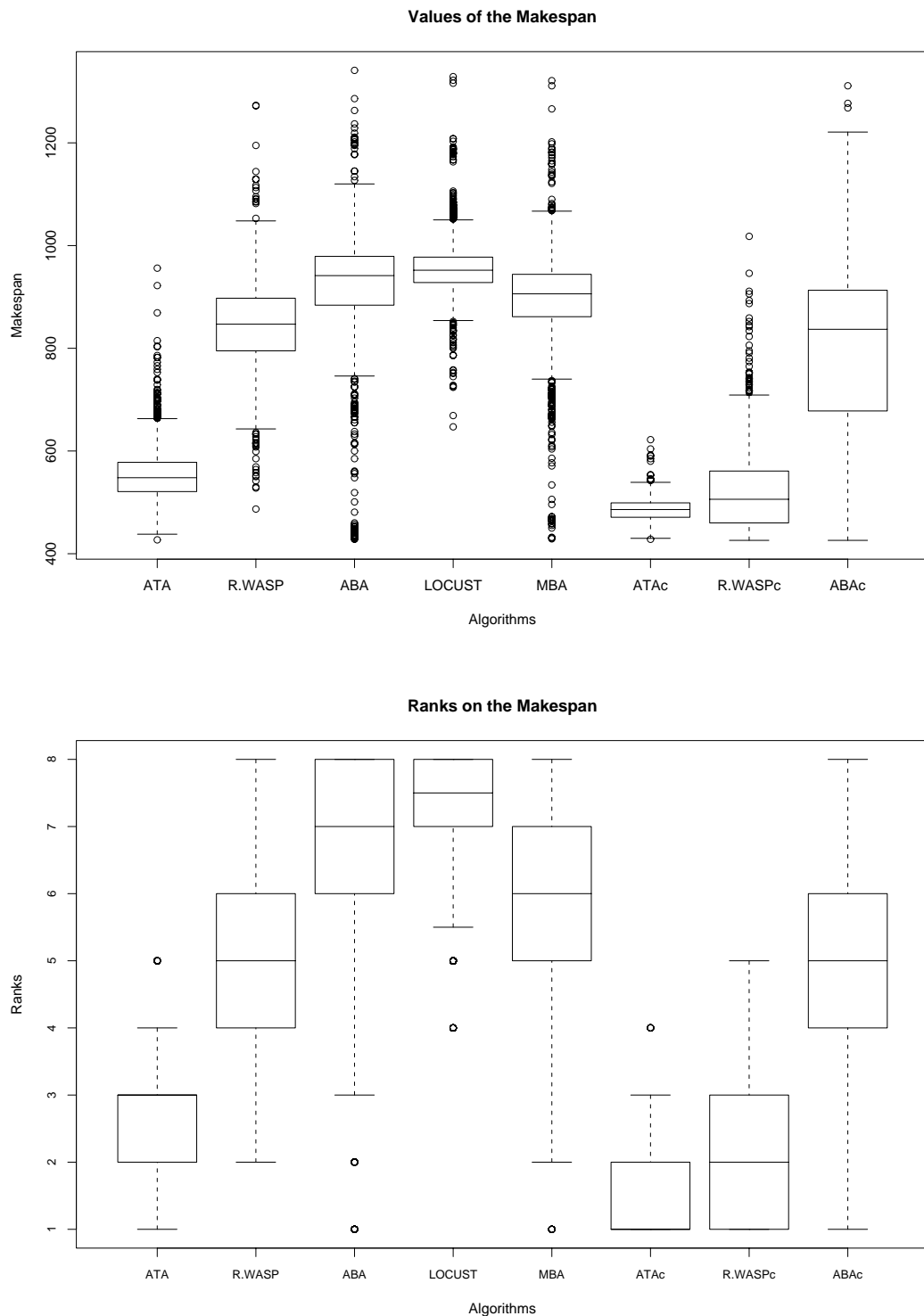


Figure 6.12: Box plot of the makespan values and ranks for all the eight algorithms run on the class of instances of the *DTA* problem. The figure confirms that *ATAc* is the algorithm that achieves the best results and that the extended algorithms perform better than the original ones. The DPS rule gives a high improvement of the performance especially to the *R-WASP* algorithm.



Table 6.8: Paired Wilcoxon Rank Sum Test applied on the makespan of the algorithms on the class of instances of the heterogeneous problem. Values are obtained considering a confidence level of 95%. The table assures that differences between algorithms on the median values are significant.

	<i>ABA</i>	<i>R-WASP</i>	<i>ABAc</i>	<i>R-WASPC</i>	<i>ATAc</i>	<i>LOCUST</i>	<i>MBA</i>
<i>R-WASP</i>	$< 2.2e^{-16}$	-	-	-	-	-	-
<i>ABAc</i>	$< 2.2e^{-16}$	$< 2.2e^{-16}$	-	-	-	-	-
<i>R-WASPC</i>	$< 2.2e^{-16}$	$< 2.2e^{-16}$	$< 2.2e^{-16}$	-	-	-	-
<i>ATAc</i>	$< 2.2e^{-16}$	$< 2.2e^{-16}$	$< 2.2e^{-16}$	$< 2.2e^{-16}$	-	-	-
<i>LOCUST</i>	$< 2.2e^{-16}$	$< 2.2e^{-16}$	$< 2.2e^{-16}$	$< 2.2e^{-16}$	$< 2.2e^{-16}$	-	-
<i>MBA</i>	$< 2.2e^{-16}$	$< 2.2e^{-16}$	$< 2.2e^{-16}$	$< 2.2e^{-16}$	$< 2.2e^{-16}$	$< 2.2e^{-16}$	-
<i>ATA</i>	$< 2.2e^{-16}$	$< 2.2e^{-16}$	$< 2.2e^{-16}$	$< 2.2e^{-16}$	$< 2.2e^{-16}$	$< 2.2e^{-16}$	$< 2.2e^{-16}$

with the DPS rule applied perform better than the respective algorithms without this rule. A deeper analysis about the makespan contribution of this rule is in the following paragraph.

To be sure of the real significance of the obtained results we applied a Wilcoxon Paired Rank Sum Test. The results presented in Table 6.8 show that different results of the makespan between algorithms are significantly different with a confidence level of 95%.

Figure 6.13 shows a box plot of the number of setups per agent and the storage dimension. Again, the trend is similar to the makespan plot of Figure 6.12. *MBA* has bad performances for setups and storage.

### The significance of the DPS rule on the *DTA* problem

The introduced rule gives a high bid probability to an agent that has a low process time for the current task. In this experiment we saved for each instance the makespan value that each algorithm achieves. For each pair of the insect-based algorithms and for each of the 1000 instances we evaluated and sorted the makespan differences. The results are presented in Figure 6.15. In most cases, differences are positive so the makespan of the original algorithm is higher than the extended algorithm. This behavior is similar for all the three algorithms considered. *R-WASPC* is the algorithm that receives the highest advantage from this rule.

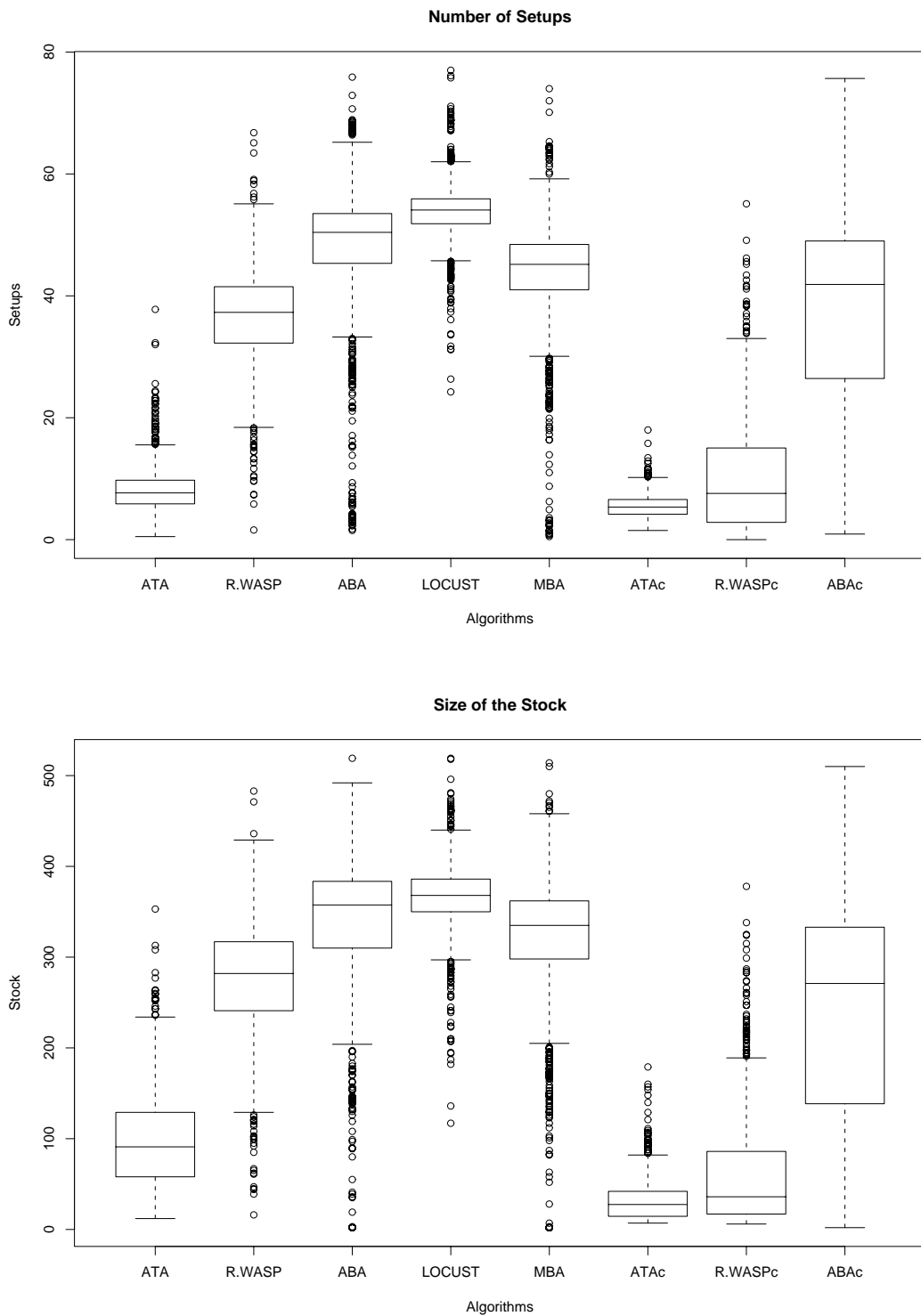


Figure 6.13: Number of setups per agent and storage dimension for the experiment with heterogeneous agents. Both graphs are similar to that in Figure 6.12. Again, values of the *ATAc* algorithm are the best ones. The *DPS* rule gives a significant increment also on these performances.

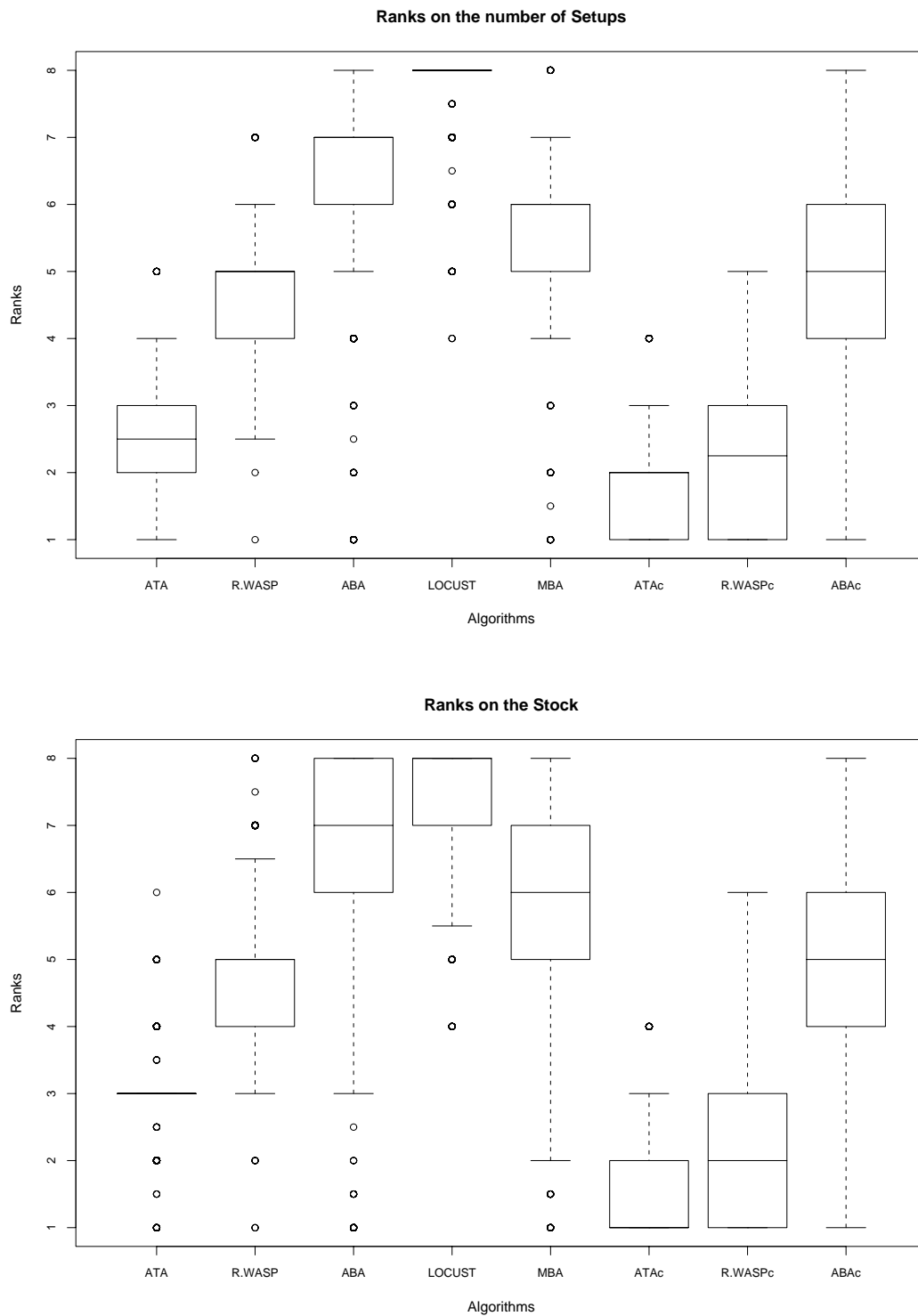


Figure 6.14: Ranks of the number of setups per agent and storage dimension for the *DTA* problem.

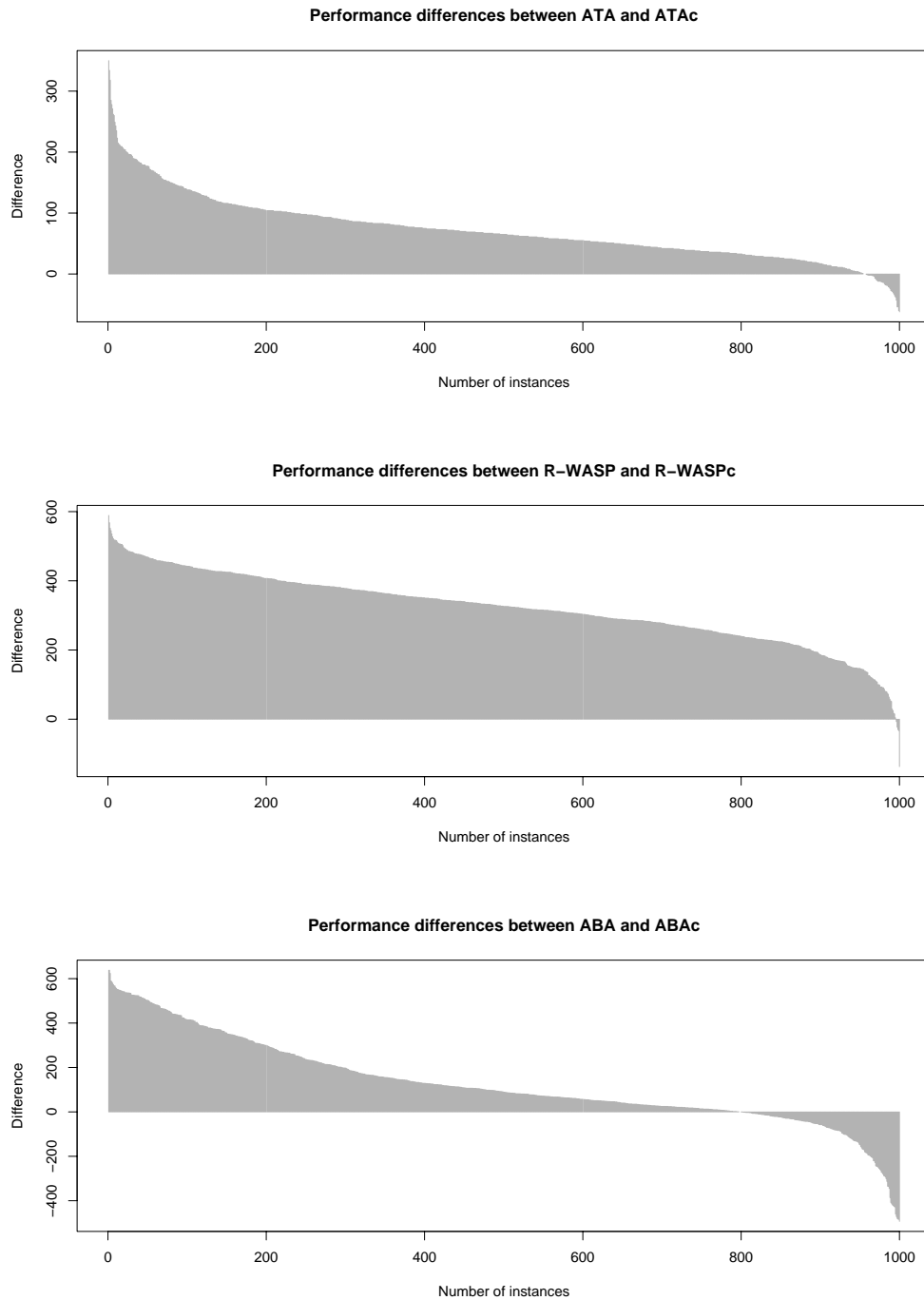


Figure 6.15: Makespan differences for the three insect-based algorithms without and with the DPS rule. The graphs show that for all the algorithms and for the major number of the 1000 instances considered the difference between the algorithm without and with the DPS rule is positive. This means that the DPS rule gives clearly a benefit to the makespan values.

# Chapter 7

## Conclusions

In this thesis we presented *Ant Task Allocation (ATA)*, an algorithm inspired by the division of labor of social insects and based on the work presented by Cicirello *et al.* [7]. *ATA* introduces four rules in order to speed up the adaptation process for particularly unpredictable instances of the homogeneous case of the *Dynamic Task Allocation (DTA)* problem. Moreover, we presented the *Different Process Speed (DPS)* rule inspired by the division of labor observed in castes of social insects and applied to all the insect-based algorithms. Its aim is to increase the performance for the heterogeneous case of the *DTA* problem. This rule takes into account the different process time that agents have for different types of tasks during the bidding process. To understand the impact of the proposed algorithm we conducted a comparison with other solutions available in the literature for the *DTA* problem. We considered two possible real-world situations: a big painting factory with identical working agents and medium factory with two heterogeneous subsets of working agents. Particular attention was put on the experimental conditions and on the statistical analysis.

We have shown that *ATA* achieves the best results for the considered class of homogeneous problems and that *ATA* with the *DPS* rule activated (*ATAc*) achieves the best results for the considered class of heterogeneous problems. We have also observed that all adaptive algorithms always achieve better results than the non-adaptive *LOCUST* algorithm. Furthermore, we have shown that the *Market Based Approach (MBA)* achieves interesting results for the homogeneous case of the problem but not for the heterogeneous case. Moreover, the performance of the insect-based algorithms are ranked according to the time they was made. In fact the algorithm of Campos' *et al.* does not obtains good results, the algorithm of Cicirello *et al.* gives a significant improvement to the performance obtained by Campos' *et al.* as they show in paper [7] and our algorithm improves again the results of the solution of Cicirello *et al.*

Another important contribution of this thesis has been the understanding the contribution of each introduced rule to the makespan. We have shown that *ATA*

with the four active rules performs better than the original algorithm proposed by Cicirello *et al.* [7]. Moreover, our results show that the introduced rule *Threshold Update Rule (TUR)* gives a large contribution to the makespan while the rule *Calculation of the Force Variable (CFV)* does not. Furthermore, also the rule *Idle Machine does not Bid (IMB)* and the rule *DOminance Contest (DOC)* bring a contribution less important than *TUR*, but still significant. Finally, we showed that the *DPS* rule significantly improves the performances of all insect-based algorithms on the heterogeneous case of the *DTA* problem.

We believe that this thesis, beside introducing some original algorithms, also gives a clear and simple methodology to perform the experiments. Furthermore, it summarizes the work made until now on the *DTA* problem.

To complete this thesis we have built a web site <http://iridia.ulb.ac.be/~rghizzioli/dta/> where it is possible to find the results, the source code of the instance generator, the algorithms and the EA tuner with interesting literature links. We hope other researchers will use this work as a starting point for new *DTA* problem extensions or to propose new algorithms to solve it.

# Annexes





# Appendix A

## The experimental environment

During the thesis work the experimental design and the software development required a significant amount of time. We developed a simulator of the algorithm that works both in command line mode and in GUI mode. Moreover, we built two instance generators. The software was written in C++ because we needed fast computation. To be able to deploy the applications on different platforms, we used the Trolltech QT API Framework. Moreover, we used the standard technology XML for the interchange of data between applications. In the following we describe the structure of the main application we developed.

### A.1 The algorithms simulator

This application meets two requirements: the performance evaluation of the presented algorithms and the tuning of their parameters. In the second case the application has to communicate with the evolutionary algorithm tuner. The core of this application is the structure of the algorithms that was built using an object-oriented paradigm. Figure A.1, according to [24], shows the UML class diagram. The software implements three main classes: *Agent* that is in charge of a booth in the *DTA* problem painting facility, *Task* that is a truck to be painted and *Algorithm* that implements methods to assign trucks to the booths. Obviously, most of the methods of these classes are abstract because they do not depend on a specific implementation. A first extension of these classes is a set of classes whose names end with *INSECT* and implement the threshold model inspired by the division of labor in social insects. The algorithms *R-WASPC* and *ABAC* extend these classes. Furthermore, *ATAc* extends *R-WASPC*. Finally, *MBA* and *LOCUST* that do not use the threshold model extend the basic classes. The simulator uses different classes able to manage the input/output. Input classes read algorithm preferences and the problem instances. Output classes write log files.

For more information about the software usage we refer to the thesis web site

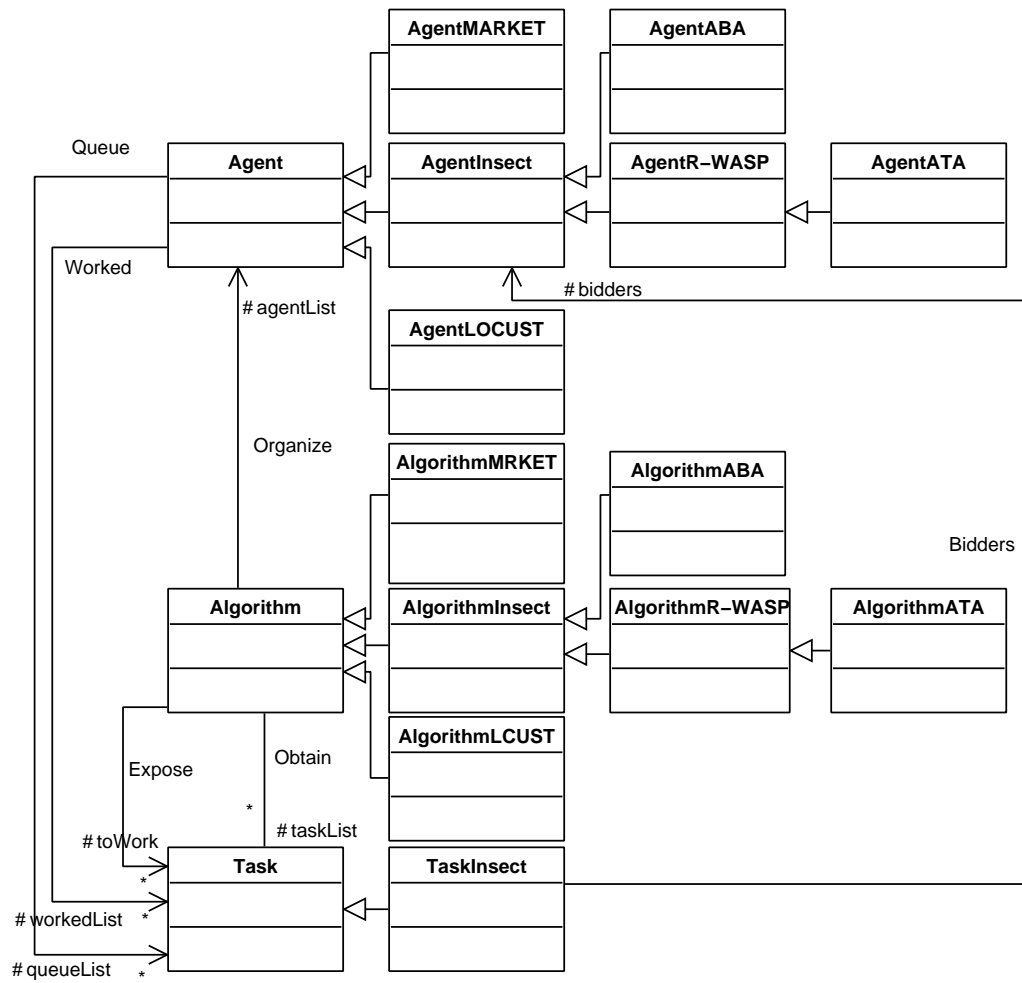


Figure A.1: UML class diagram of the simulator.

at the address <http://iridia.ulb.ac.be/~rghizzioli/dta/>.



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